Stacks and Queues

Week 9
Gaddis: Chapter 18

CS 5301
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Introduction to the Stack

- **Stack**: a data structure that holds a collection of elements of the same type.
  - The elements are accessed according to LIFO order: last in, first out
  - No random access to other elements

- **Examples**:
  - plates in a cafeteria
  - bangles . . .

Stack Operations

- **Operations**:
  - **push**: add a value onto the top of the stack
    - make sure it’s not full first.
  - **pop**: remove (and return) the value from the top of the stack
    - make sure it’s not empty first.
  - **isFull**: true if the stack is currently full, i.e., has no more space to hold additional elements
  - **isEmpty**: true if the stack currently contains no elements

Stack illustrated

```c
int item;
stack.push(2);
stack.push(3);
stack.push(5);
item = stack.pop(); //item is 5
item = stack.pop(); //item is 3
stack.push(10);
```
Implementing a Stack Class

- Array implementations:
  - fixed size (static) arrays: size doesn't change
  - dynamic arrays: can resize as needed in push

- Linked List
  - grow and shrink in size as needed

- Templates
  - any of the above can be implemented using templates

A static stack class

class IntStack
{
private:
  const static int STACKSIZE = 100; // The stack size
  int stackArray[STACKSIZE]; // The stack array
  int top; // Index to the top of the stack
public:
  // Constructor
  IntStack() { top = -1; } // empty stack
  // Stack operations
  void push(int);
  int pop();
  bool isFull() const;
  bool isEmpty() const;
};

A static stack class: push&pop

//*****************************************************
// Member function push pushes the argument onto *
// the stack.                                       *
//*****************************************************
void IntStack::push(int num)
{
  assert(!isFull());
  top++;
  stackArray[top] = num;
}

//*****************************************************
// Member function pop pops the value at the top *
// of the stack off, and returns it.                *
//*****************************************************
int IntStack::pop()
{
  assert(!isEmpty());
  int num = stackArray[top];
  top--;
  return num;
}

A static stack class: functions

//*******************************************************************************
// Member function isFull returns true if the stack *
// is full, or false otherwise.                                                *
//*******************************************************************************
bool IntStack::isFull() const
{
  return (top == STACKSIZE - 1);
}

//*******************************************************************************
// Member function isEmpty returns true if the stack *
// is empty, or false otherwise.                                              *
//*******************************************************************************
bool IntStack::isEmpty() const
{
  return (top == -1);
}
A Dynamic Stack Class:  
Linked List implementation

- Push and pop from the head of the list:

```cpp
//*************************************************
// Member function push pushes the argument onto * 
// the stack.                                     *
//*************************************************
void DynIntStack::push(int num) {
    assert(!isFull());
    Node *temp = new Node;
    temp->data = num;
    //insert at head of list
    temp->next = head;
    head = temp;
}
```

```cpp
private:
    struct Node {
        int data;
        Node* next;
    };
    Node* head; // ptr to top
```

- Push and pop from the head of the list:

```cpp
//*************************************************
// Member function pop pops the value at the top * 
// of the stack off, and returns it.              *
//*************************************************
int DynIntStack::pop() {
    assert(!isEmpty());
    int result = head->data;
    Node * temp = head;
    head = head->next;
    delete temp;
    return result;
}
```

```cpp
private:
    struct Node {
        int data;
        Node* next;
    };
    Node* head; // ptr to top
```

Introduction to the Queue

- **Queue**: a data structure that holds a collection of elements of the same type.
  - The elements are accessed according to FIFO order: first in, first out
  - No random access to other elements

- **Examples:**
  - people in line at a theatre box office
  - restocking perishable inventory

Queue Operations

- **Operations:**
  - **enqueue**: add a value onto the rear of the queue (the end of the line)
    - make sure it’s not full first.
  - **dequeue**: remove a value from the front of the queue (the front of the line) “Next!”
    - make sure it’s not empty first.
  - **isFull**: true if the queue is currently full, i.e., has no more space to hold additional elements
  - **isEmpty**: true if the queue currently contains no elements
Queue illustrated

Implementing a Queue Class

Same as for Stacks:
- Array implementations:
  - fixed size (static) arrays: size doesn’t change
  - dynamic arrays: can resize as needed in enqueue
- Linked List
  - grow and shrink in size as needed
- Templates
  - any of the above can be implemented using templates

Implementing a Queue: Array

- When front and rear indices move in the array:
  - problem: rear hits end of array quickly
  - solution: “circular array”: wrap index around to front of array

  ```
  int item;
  q.enqueue(2);
  q.enqueue(3);
  q.enqueue(5);
  item = q.dequeue(); //item is 2
  item = q.dequeue(); //item is 3
  q.enqueue(10);
  ```

Implementing a Queue: Array

- To “wrap” the rear index back to the front of the array, you can use this code to increment rear during enqueue:

  ```
  if (rear == queueSize-1)
    rear = 0;
  else
    rear = rear+1;
  ```

  The following code is equivalent, but shorter (assuming 0 <= rear < queueSize):

  ```
  rear = (rear + 1) % queueSize;
  ```

- Do the same for advancing the front index.
Implementing a Queue: Array

- When is it full? \((\text{rear}+1) \mod \text{queueSize} = \text{front}\)

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- When is it empty? \((\text{rear}+1) \mod \text{queueSize} = \text{front}\)

-one element left:

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-no elements left, front passes rear:

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- Don’t use rear and front to determine if the queue is full or empty!!

A static queue class

```cpp
class IntQueue {
    private:
        const static int QUEUESIZE = 100;  // capacity of queue
        int queueArray[QUEUESIZE];  // The queue array
        int front;  // Subscript of the queue front
        int rear;  // Subscript of the queue rear
        int numItems;  // Number of items in the queue
    public:
        // Constructor
        IntQueue() { front = 0;  rear = -1;  numItems = 0;  }

        // Queue operations
        void enqueue(int num);
        int dequeue();
        bool isEmpty() const;
        bool isFull() const;
};
```

A static queue: enqueue/dequeue

```cpp
//***************************************
// Enqueue inserts a value at the rear of the queue. *
//***************************************
void IntQueue::enqueue(int num)
{
    assert(!isFull());
    rear = (rear + 1) % QUEUESIZE;
    queueArray[rear] = num;
    numItems++;
}
```

```cpp
//***************************************
// Dequeue removes the value at the front of the queue and returns the value. *
//***************************************
int IntQueue::dequeue()
{
    assert(!isEmpty());
    int result = queueArray[front];
    front = (front + 1) % QUEUESIZE;
    numItems--;
    return result;
}
```

A static queue class: functions

```cpp
//***************************************
// isEmpty returns true if the queue is empty *
//***************************************
bool IntQueue::isEmpty() const {
    return (numItems == 0);  
}
```

```cpp
//***************************************
// isFull returns true if the queue is full *
//***************************************
bool IntQueue::isFull() const {
    return (numItems == QUEUESIZE);
}
```
A Dynamic Queue Class: Linked List implementation

- Use pointers `front` and `rear` to point to first and last elements of the list:

```
front -> rear -> NULL
```

- Enqueue at the rear of the list, dequeue from the front:

```
void DynIntQueue::enqueue(int num) {
    assert(!isFull());
    Node *temp=new Node;
    temp->data = num;
    temp->next = NULL;
    //append to rear of list, reset rear
    if (isEmpty())
        front = rear = temp;
    else {
        rear->next = temp;
        rear = temp;
    }
}
```

```
private:
    struct Node {
        int data;
        Node* next;
    };
    Node* front; // ptr to first
    Node* rear; // ptr to last
```

```
A Dynamic Queue Class: Linked List implementation

- Enqueue at the rear of the list, dequeue from the front:

```
int DynIntQueue::dequeue() {
    assert(!isEmpty());
    int value = front->data;
    // remove the first node (front)
    Node *temp = front;
    front = front->next;
    delete temp;
    if (front==NULL) rear = NULL;
    return value;
}
```

```
private:
    struct Node {
        int data;
        Node* next;
    };
    Node* front; // ptr to first
    Node* rear; // ptr to last
```