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- Very simple method.
- Compare first element to target value, if not found then compare second element to target value . . .
- Repeat until: target value is found (return its index) or we run out of items (return -1).

first attempt int searchList (int list[], int size, int target) {

int position = -1; //position of target
for (int i=0; i<size; i++)
{
 if (list[i] == target) //found the target!
 position = i; //record which item
}
return position;</pre>

Is this algorithm correct (does it calculate the right value)?

Is this algorithm efficient (does it do unnecessary work)?

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Linear Search in C++

```
int searchList (int list[], int size, int target) {
    int position = -1; //position of target
    bool found = false; //flag, true when target is found
    for (int i=0; i < size && !found; i++)
    {
        if (list[i] == target) //found the target!
        {
            found = true; //set the flag
            position = i; //record which item
        }
    }
    return position;
}</pre>
```

Is this algorithm correct (does it calculate the right value)?

Is this algorithm efficient (does it do unnecessary work)?

Evaluating the Algorithm

- Does it do any unnecessary work?
- Is it time efficient? How would we know?
- We measure time efficiency of algorithms in terms of number of main steps required to finish.
- For search algorithms, the main step is comparing an array element to the target value.

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- Number of steps depends on:
 - size of input array
 - whether or not value is in array
 - where the value is in the array

Program that uses linear search

```
#include <iostream>
using namespace std;
int searchList(int[], int, int);
int main() {
  const int SIZE=5;
  int idNums[SIZE] = {871, 750, 988, 100, 822};
 int results, id;
  cout << "Enter the employee ID to search for: ";
  cin >> id;
  results = searchList(idNums, SIZE, id);
 if (results == -1) {
   cout << "That id number is not registered\n";</pre>
  } else {
    cout << "That id number is found at location ";
    cout << results+1 << endl;</pre>
}
                                                             6
```

Efficiency of Linear Search

how many main steps (comparisons to target)?

N is the number of elements in the array

	N=50,000	In terms of N
Best Case:	1	1
Average Case:	25,000	N/2
Worst Case:	50,000	N

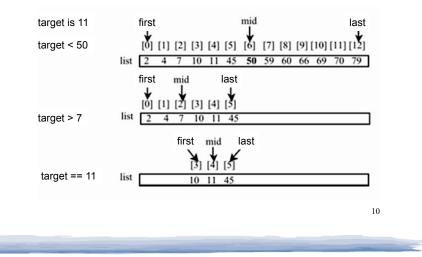
Note: if we search for many items that are not in the array, the average case will be greater than N/2.

Binary Search

- Works only for SORTED arrays
- Divide and conquer style algorithm
- Compare target value to middle element in list.
 - if equal, then return its index
 - if less than middle element, repeat the search in the first half of list
 - if greater than middle element, repeat the search in last half of list
- If current search list is narrowed down to 0 elements, return -1 9

Binary Search Algorithm example

We use first and last to indicate beginning and end of current search list



Binary Search in C++

```
int binarySearch (int array[], int size, int target) {
  int first = 0.
                         //index of beginning of search list
      last = size - 1, //index of end of search list
     middle,
                         //index of midpoint of search list
      position = -1;
                         //position of target value
  bool found = false;
                           //flag
  while (first <= last && !found) {</pre>
    middle = (first + last) /2;
                                     //calculate midpoint
    if (array[middle] == target) {
                                                What if first + last is odd?
     found = true;
                                                What if first==last?
      position = middle;
    } else if (target < array[middle]) {</pre>
      last = middle -1;
                                  //search list = lower half
     else {
      first = middle + 1;
                                  //search list = upper half
  return position;
                                                          11
```

Program using Binary Search

```
#include <iostream>
using namespace std;
int binarySearch(int[], int, int);
                                                How is this program different
                                               from the one on slide 6?
int main() {
  const int SIZE=5;
  int idNums[SIZE] = {100, 750, 822, 871, 988};
  int results, id;
  cout << "Enter the employee ID to search for: ";
  cin >> id;
  results = binarySearch(idNums, SIZE, id);
  if (results == -1) {
    cout << "That id number is not registered\n";</pre>
  } else {
   cout << "That id number is found at location ":
    cout << results+1 << endl;</pre>
 }
                                                              12
```

}

Efficiency of Binary Search			
Calcu	Calculate worst case (target not in list) for N=1024		
[# Items left to search	# Comparisons so far	
	1024	0	
	512	1	
_	256	2	
	128	3	
	64	4	
	32	5	
	16	6	-
	8	7	
	4	8	-
	2	9	Goal: calculate
	1	10 +	this value from N
	1024 = 2 ¹⁰ <==>	$\log_2 1024 = 10$	- 13

Efficiency of Binary Search

If N is the number of elements in the array, how many comparisons (steps)?

1024 = 2	¹⁰ <==> lo	g ₂ 1024 = 10]
$N = 2^{steps}$ <==> $log_2 N = steps$		To what power do I raise 2 to get N?	
	N-50 000	In terms of N	
	11-30,000		·
Best Case:	1	1	
Worst Case:	16	log ₂ N	Rounded up to next whole number
0036.			14

Is Log₂N better than N?

Is binary search better than linear search?

Is this really a fair comparison?

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Compare values of N/2, N, and Log₂ N as N increases:

Ν	N/2	Log ₂ N
5	2.5	2.3
50	25	5.6
500	250	9
5,000	2,500	12.3
50,000	25,000	15.6

N and N/2 are growing much faster than log N!

slower growing is more efficient (fewer steps).

8.3 Sorting Algorithms

- Sort: rearrange the items in an array into ascending or descending order.
- Bubble Sort
- Selection Sort



55 112 78 14 20 179 42 67 190 7 101 1 122 170 8 unsorted sorted

1 7 8 14 20 42 55 67 78 101 112 122 170 179 190

The Bubble Sort

- On each pass:
 - Compare first two elements. If the first is bigger, they exchange places (swap).
 - Compare second and third elements. If second is bigger, exchange them.
 - Repeat until last two elements of the list are compared.
- Repeat this process (keep doing passes) until a pass completes with no exchanges

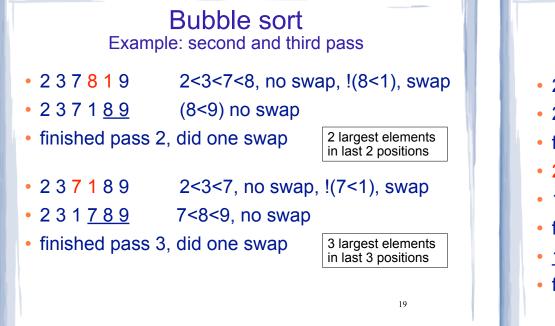
Bubble sort Example: first pass

• 723891	7 > 2, swap
• 273891	7 > 3, swap
• 237891	!(7 > 8), no swap
• 237 <mark>89</mark> 1	!(8 > 9), no swap
• 2 3 7 8 <mark>9 1</mark>	9 > 1, swap
• 2 3 7 8 1 <u>9</u>	finished pass 1, did 3 swaps

Note: largest element is now in last position

Note: This is one complete pass!

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Bubble sort Example: passes 4, 5, and 6

- 2 <mark>3 1</mark> 7 8 9
- 2<3, !(3<1) swap, 3<7<8<9
- 2 1 <u>3 7 8 9</u>
- finished pass 4, did one swap
- 2 1 3 7 8 9 !(2<1) swap, 2<3<7<8<9
- 1 <u>2 3 7 8 9</u>
- finished pass 5, did one swap
- <u>1 2 3 7 8 9</u> 1<2<3<7<8<9, no swaps
- finished pass 6, no swaps, list is sorted!

Bubble sort how does it work?

- At the end of the first pass, the largest element is moved to the end (it's bigger than all its neighbors)
- At the end of the second pass, the second largest element is moved to just before the last element.
- The back end (tail) of the list remains sorted.
- Each pass increases the size of the sorted portion.

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 No exchanges implies each element is smaller than its next neighbor (so the list is sorted).

Bubble Sort in C++

<pre>void bubbleSort (int array[], int size) {</pre>
<pre>bool swap; int temp;</pre>
do {
<pre>swap = false; for (int i = 0; i < (size-1); i++) {</pre>
<pre>if (array [i] > array[i+1]) {</pre>
<pre>temp = array[i]; array[i] = array[i+1]; array[i+1] = temp; swap = true;</pre>
}
<pre>} while (swap); }</pre>

Program using bubble sort

<pre>#include <iostream> using namespace std;</iostream></pre>	
<pre>void bubbleSort(int [], int); void showArray(int [], int);</pre>	
<pre>int main() { int values[6] = {7, 2, 3, 8, 9, 1};</pre>	
<pre>cout << "The unsorted values are: \n"; showArray (values, 6);</pre>	
<pre>bubbleSort (values, 6);</pre>	
<pre>cout << "The sorted values are: \n"; showArray(values, 6); }</pre>	Output: The unsorted values are: 7 2 3 8 9 1
<pre>void showArray (int array[], int size) { for (int i=0; i<size; "="" ";<="" <<="" array[i]="" cout="" i++)="" pre=""></size;></pre>	The sorted values are: 1 2 3 7 8 9
<pre>cout << endl; }</pre>	
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Selection Sort

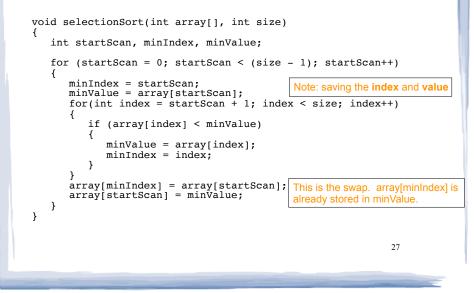
- There is a pass for each position (0..size-1)
- On each pass, the smallest (minimum) element in the rest of the list is exchanged (swapped) with element at the current position.
- The first part of the list (the part that is already processed) is always sorted
- Each pass increases the size of the sorted portion.

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Selection Sort in C++ Selection sort Mv version Example // Returns the index of the smallest element, starting at start int findIndexOfMin (int array[], int size, int start) { • 7 2 3 8 9 1 1 is the min a[5], swap with a[0] int minIndex = start; for (int i = start+1; i < size; i++) { Note: saving the **index** if (array[i] < array[minIndex]) {</pre> • 1 2 3 8 9 7 2 is the min a[1], self-swap a[1] minIndex = i;• 1 2 3 8 9 7 3 is the min a[2], self-swap a[2] We need to find the **index** of the minimum return minIndex; value so that we can do the swap } • 123897 7 is the min a[5], swap with a[3] // Sorts an array, using findIndexOfMin void selectionSort (int array[], int size) { 8 is the min a[5], swap with a[4] • 1 2 3 7 9 8 int temp: int minIndex; for (int index = 0; index < (size -1); index++) {</pre> 123789 sorted minIndex = findIndexOfMin(array, size, index); //swap temp = array[minIndex]; array[minIndex] = array[index]; Note: underlined portion of list is sorted. array[index] = temp; Note: This is five passes 25 26

}

Selection Sort in C++ Gaddis version



Program using Selection Sort

```
#include <iostream>
using namespace std;
int findIndexOfMin (int [], int, int);
void selectionSort(int [], int);
void showArray(int [], int);
int main() {
   int values[6] = {7, 2, 3, 8, 9, 1};
   cout << "The unsorted values are: \n";
   showArray (values, 6);
   selectionSort (values, 6);
   cout << "The sorted values are: \n":
                                                Output:
   showArray(values, 6);
                                                 The unsorted values are:
                                                 723891
                                                 The sorted values are:
void showArray (int array[], int size) {
   for (int i=0; i<size; i++)</pre>
                                                 123789
      cout << array[i] << " ";</pre>
   cout << endl;
                                                          28
```

Analysis of Algorithms using Big O notation

- Which algorithm is better, linear search or binary search?
- Which algorithm is better, bubble sort or selection sort?
- How can we answer these questions?
- Analysis of algorithms is the determination of the amount of resources (such as time and storage) necessary to execute them.

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Time Efficiency of Algorithms

- To classify the time efficiency of an algorithm:
 - Express "time" (using number of main steps), as a mathematical function of input size (or n below).

Binary search: $f(n) = \log_2(n)$

- Need a way to be able to compare these math functions to determine which is better.
 - We are mostly concerned with which function has smaller values (# of steps) at very large data sizes.
 - We compare the growth rates of the functions and prefer the one that grows more slowly.

Classifications of (math) functions

Constant	f(x)=b	O(1)
Logarithmic	$f(x)=log_b(x)$	O(log n)
Linear	f(x)=ax+b	O(n)
Linearithmic	$f(x)=x \log_b(x)$	O(n log n)
Quadratic	f(x)=ax ² +bx+c	O(n²)
Exponential	f(x)=2 ^x	O(2 ⁿ)

- Last column is "big O notation", used in CS.
- It ignores all but dominant term, constant factors

