## Sets \& Hash Tables

Week 13
Weiss: chapter 20
CS 5301
Spring 2018
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## Set Operations

- Set construction
the empty set (0 elements in the set)
- isEmpty()

True, if the set is empty; false, otherwise.

- Insert(element)
- If element is already in the set, do nothing; otherwise add it to the set
- Delete(element)

If element is not a member of the set, do nothing; otherwise remove it from the set.

## What are sets?

- A set is a collection of objects of the same type that has the following two properties:
- there are no duplicates in the collection
- the order of the objects in the collection is irrelevant.
- $\{6,9,11,-5\}$ and $\{11,9,6,-5\}$ are equivalent.
- There is no first element, and no successor of 9 .


## Set Operations

- Member(element): boolean
- True, if element is a member of the set; false, otherwise
- Union(Set1,Set2): Set
- returns a Set containing all elements of the two Sets, no duplications.
- Intersection(Set1,Set2): Set
- returns a Set containing all elements common to both sets.


## Set Operations

- Difference(Set1,Set2): Set
- returns a Set containing all elements of the first set except for the elements that are in common with the second set.
- Subset(Set1,Set2): boolean

True, if Set1 is a subset of Set2 (if all elements of the Set1 are also elements of Set2).

- Equals(Set1,Set2): boolean

True, if both sets contain exactly the same elements.

## Implementation

- Array of elements implementation: member

```
bool member(int x) {
    or (int i=0; i<count; i++) {
        if (intSet[i]==x)
            return true;
    }
    return false;
```

- Array of elements implementation: union

IntSet operator+(IntSet rhs) \{
IntSet newSet;
for (int i=0; i<count; i++)
newSet.insert(intSet[i]);
for (int i=0; i<rhs.count; i++)
newSet.insert(rhs.intSet[i])
return newSet;
Exercise: implement all of the set operations for the IntSet.

## Implementation

- Array of elements implementation
- each element of the set will occupy a position in the array.
the member (find) operation will be inefficient, must use linear search.

```
class IntSet {
    int count; //number of elements in the set, set to 0 in constr
    int intSet[100]; //stores the elements in positions 0..count
```

- insert must not add duplicates:

```
void insert(int x) {
    if (!member(x) && coun
        intSet [cou
    }
```

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## What are hash tables?

- A Hash Table is used to implement a set (or a search table), providing basic operations in constant time (no loops/recursion):
- insert
- delete (optional)
- find (also called "member")
- makeEmpty (need not be constant time)
- It uses a function that maps an object in the set (a key) to its location in the table.
- The function is called a hash function.


## Using a hash function

## Placing elements in the array



## How to resolve the collision?

Next place part number 6702 in the array.

Hash(partNum) = partNum \% 100
$6702 \% 100=2$
But values[2] is already occupied.

COLLISION OCCURS


One way is by linear probing. This uses the following function
(HashValue + 1) \% 100
repeatedly until an empty location is found for part number 6702.

## Collision resolved



$$
(\operatorname{Hash}(6702)+1) \% 100=3
$$

But values[3] is already occupied.

$$
(\operatorname{Hash}(6702)+2) \% 100=4
$$

Part 6702 can be placed at the location with index 4.

## Collision resolved

|  | values |
| :---: | :---: |
| [0] | Empty |
| [1] | 4501 |
| [2] | 5502 |
| [3] | 7803 |
| [4] | 6702 |
| - | - |
| - |  |
| [ 97] | Empty |
| [98] | 2298 |
| [99] | 3699 |

Part 6702 is placed at the location with index 4.

Where would the part with number 4598 be placed using linear probing?

## Implementation

- Simple array implementation
- keys are ints, all greater than or equal to 0 :

```
class HashTable {
private:
    int *array;
    nt size; // use -1 to indicate empty slot
    int hash (int key) ; // maps key to position in array
public:
    HashTable (int size); //initialize all elements to -1
    ~HashTable();
    bool find(int);
    void insert (int)
    void display();
//return true if int in table
//add int to table
//show elements in table
```


## Hashing concepts

- Hash Table: (usually an array) where objects are stored according to their key
key: attribute of an object used for searching/ sorting
- number of valid keys usually greater than number of slots in the table
number of keys in use usually much smaller than table size.
- Hash function: maps a key to a Table index
- Collision: when two separate keys hash to the same location


## Implementation

- Simple array implementation:

```
HashTable::HashTable (int s) {
    size = s;
    array = new int[size]; //dynamic allocation
    for (int i=0; i<size; i++) { //set all values to -1
        array[i] = -1;
    }
}
int HashTable::hash(int key) {
    return key % size;
}
void HashTable::insert ( int element) {
    int index = hash(element); //linear probing, if not at index
    while (array[index]!=-1 && array[index] != element) {
        index = (index+1)%size;
    }
    array[index] = element;
                            //puts element at first open slot
```


## Collision Resolution:

## Linear Probing

- Insert: When there is a collision, search sequentially for the next open slot (-1)
- Put the value in the table at that position
- Find: if the key is not at the hashed location, keep searching sequentially for it.
if it reaches an open slot (-1), the key is not found
- Remove: if the key is not at the hashed location, keep searching sequentially for it.
if the key is found, set the status to -1
- Problem: Removing an element in the middle of a chain. The Find method needs to know to keep searching to the end of the chain.


## Implementation

- Array of linked lists implementation

The data structure:

```
class ChainedTable {
private:
    static const int SIZE = 10;
    struct Node {
        int key;
        node *nextNode;
    };
    Node* table[SIZE]; //array of pointers to Nodes
    int hash (int key) ; // maps key to position in array
public:
    ChainedTable(); //inits all pointers in array to NULL
    bool find(int); //return true if int in table
    void insert (int); //add int to table
};
```


## Collision Resolution: <br> Separate chaining

- Use an array of linked lists for the hash table
- Each linked list contains all objects that hashed to that location
no collisions

Hash function is still: $h(K)=k \% 10$


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## Separate Chaining

- To insert a an object:
- compute hash(k)
- if the object is not already in the list at that location, insert the object into the list.
- To find an object:
compute hash(k)
- search the linked list there for the key of the object
- To delete an object:
compute hash(k)
search the linked list there for the key of the object
if found, remove it

