

# Data Flow Coverage

# Control-Flow-Graph-Based Coverage Criteria

- **Statement Coverage**
- **Path Coverage**
- **Branch Coverage**
- **Hidden Paths**
- **Loop Guidelines**
  - **General**
  - **Boundary - Interior**

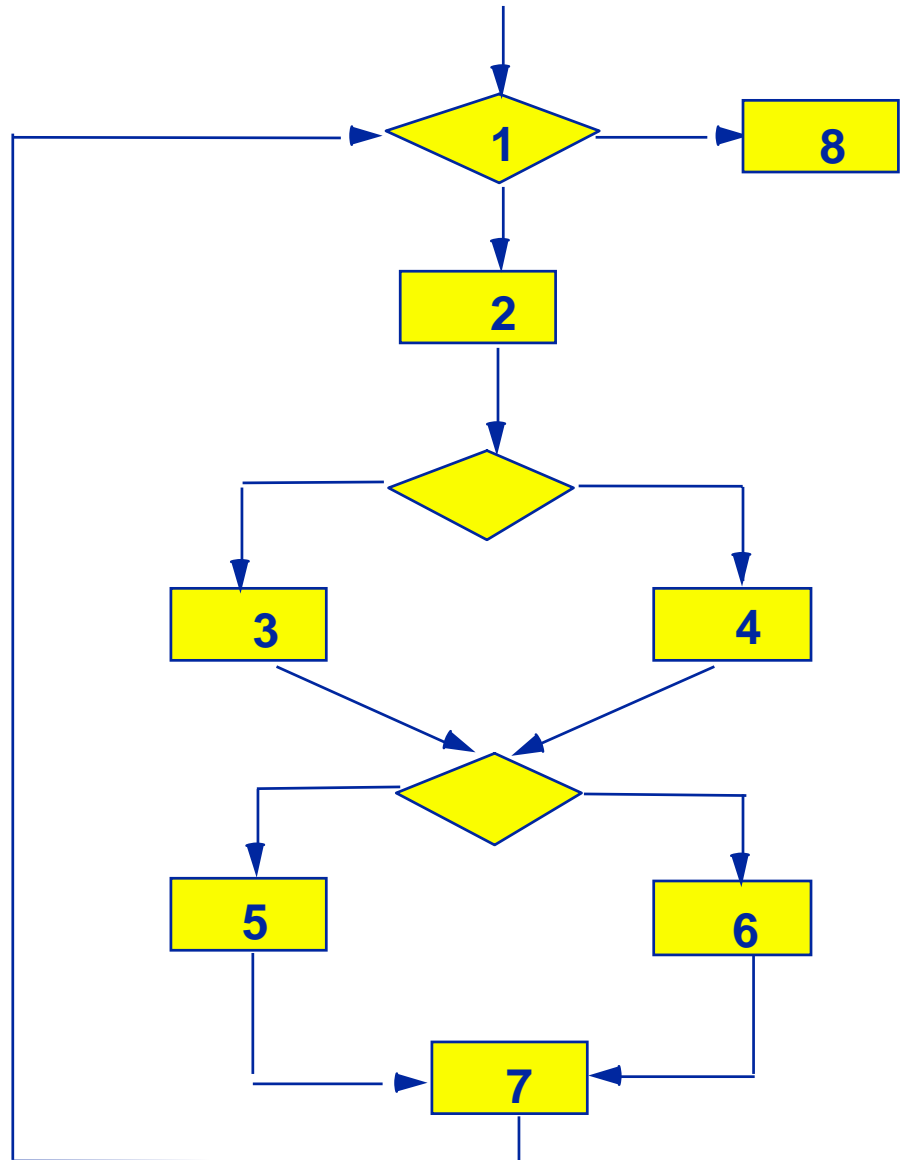
# Paths for Example

## Boundary paths

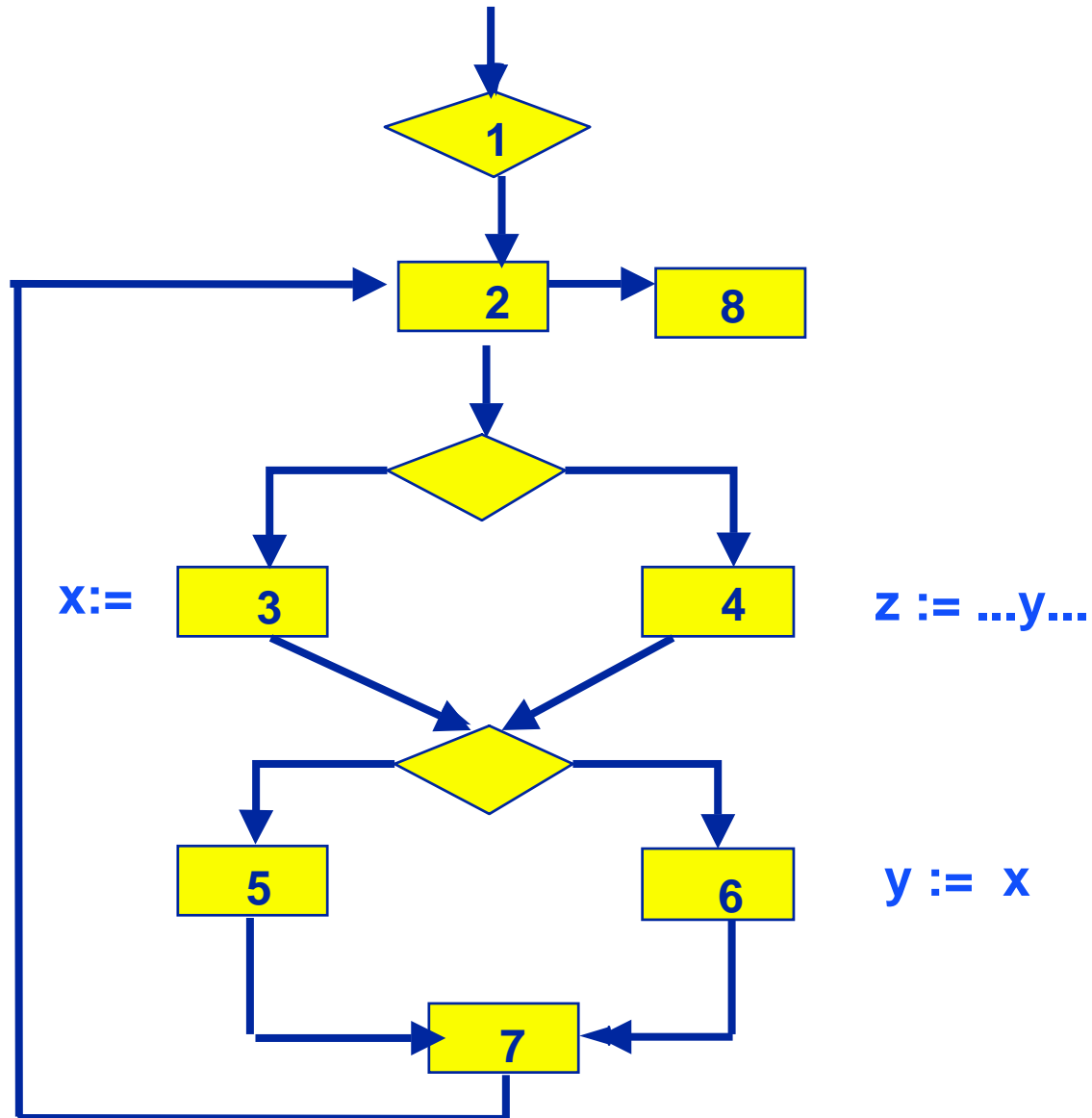
1,2,3,5,7	a
1,2,3,6,7	b
1,2,4,5,7	c
1,2,4,6,7	d

## Interior paths (for 2 executions of the loop)

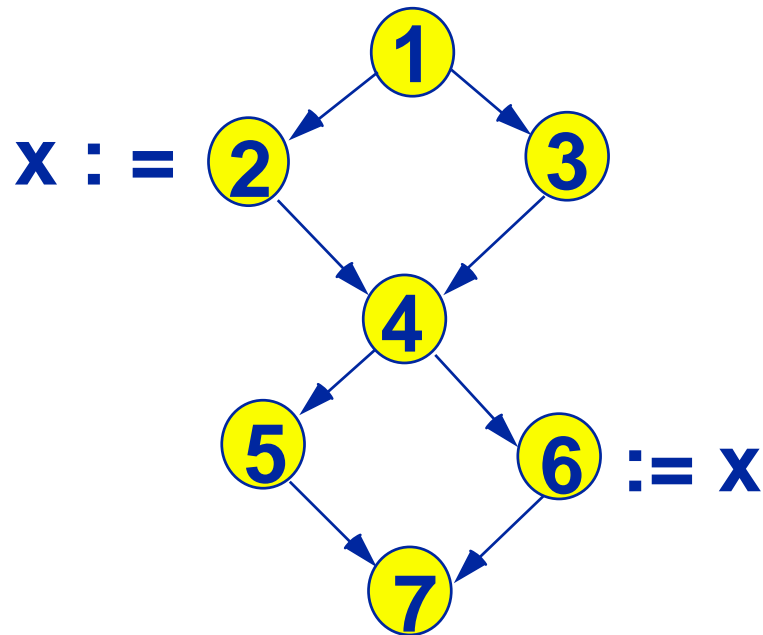
a,a  
a,b  
a,c  
a,d  
b,a  
b,b  
...  
x,y for x,y = a, b, c, d



# Need Control Flow **AND** Data Dependence



# Non-looping Path Selection Problem



All branches      1, 2, 4, 5, 7  
                         1, 3, 4, 6, 7

does not exercise the relationship between the definition of  $X$  in statement 2 and the reference to  $X$  in statement 6.

# Definitions

- $d_n(x)$  denotes that variable  $x$  is assigned a value at node  $n$  (**defined**)
- $u_m(y)$  denotes that variable  $y$  is **used** (referenced at node  $m$ )
  - a **definition clear path**  $p$  with respect to (wrt)  $x$  is a subpath where  $x$  is not defined at any of the nodes in  $p$
  - a definition  $d_m(x)$  **reaches** a use  $u_n(x)$  iff there is a subpath  $(m) \bullet p \bullet (n)$  such that  $p$  is definition clear wrt  $x$

# Data Flow Path Selection

- **Rapps and Weyuker**
  - definition-clear subpaths from definitions to uses
- **Ntafos**
  - chains of alternating definitions and uses linked by definition-clear subpaths
- **Laski and Korel**
  - combinations of definitions that reach uses at a node via a subpath

## Assumptions

- no edges of the form  $(n, n_s)$  or  $(n_f, n)$
- no edges of the form  $(n, n)$
- there is at most one edge  $(m, n)$  for all  $m, n$
- every control graph is well formed
  - Connected
  - Single start and single final node
- every loop has a single entry and a single exit



## More assumptions

- at least one variable is associated with a node representing a predicate
- no variable definitions are associated with a node representing a predicate
- every definition of a variable reaches at least one use of that variable
- every use is reached by at least one definition
- every control graph contains at least one variable definition
- no variable uses or definitions are associated with  $n_s$  and  $n_f$

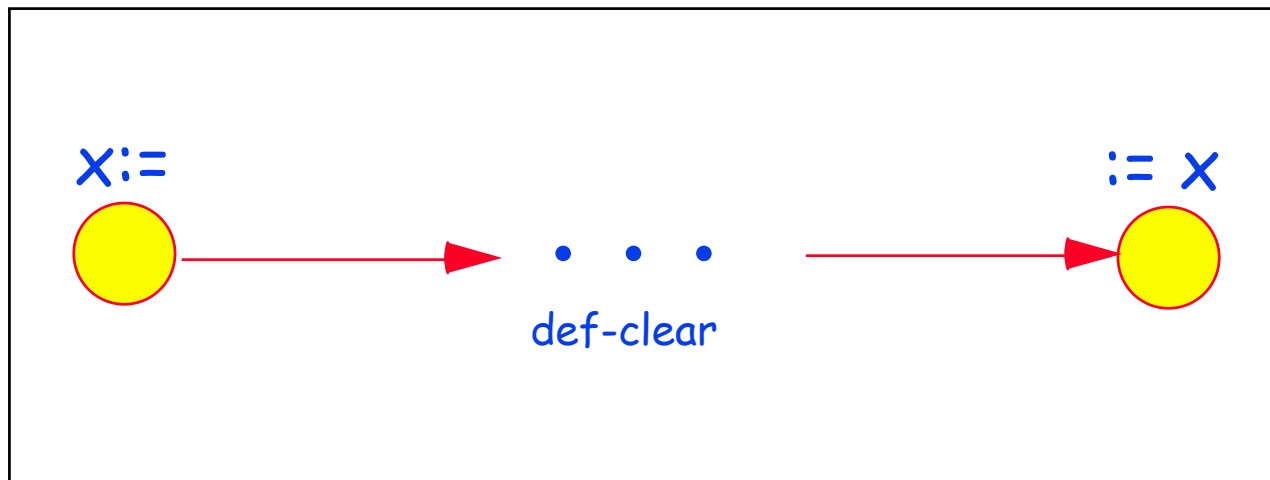
# Rapps' and Weyuker's Data Flow Criteria

## Foundation:

- Definition-clear subpaths from each definition to {some/all} use(s)

## All-Defs

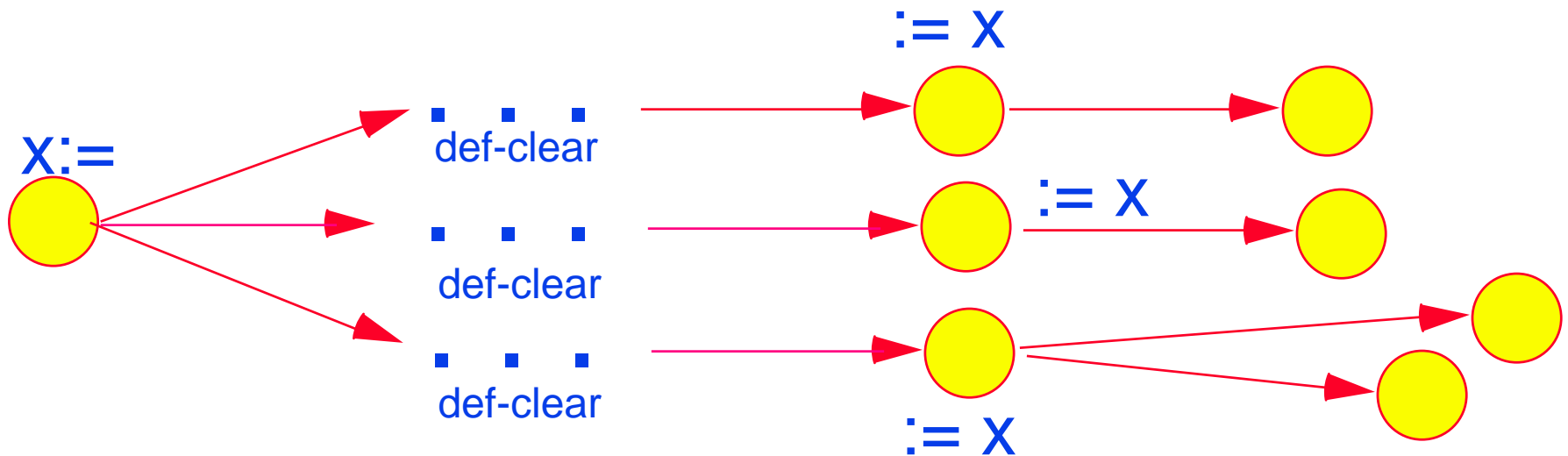
- Some definition-clear subpath **from each definition to some use** reached by that definition



# Rapps' and Weyuker's Data Flow Criteria

## All-Uses

- Some definition-clear subpath from each definition to **each use reached by that definition** and each successor node of the use



# Rapps' and Weyuker's Data Flow Criteria

C-use is a "computation use"

P-use is a "predicate use"

## All-C-Uses, Some-P-Uses

- either All-C-Uses for  $d_m(x)$  or at least one P-Use

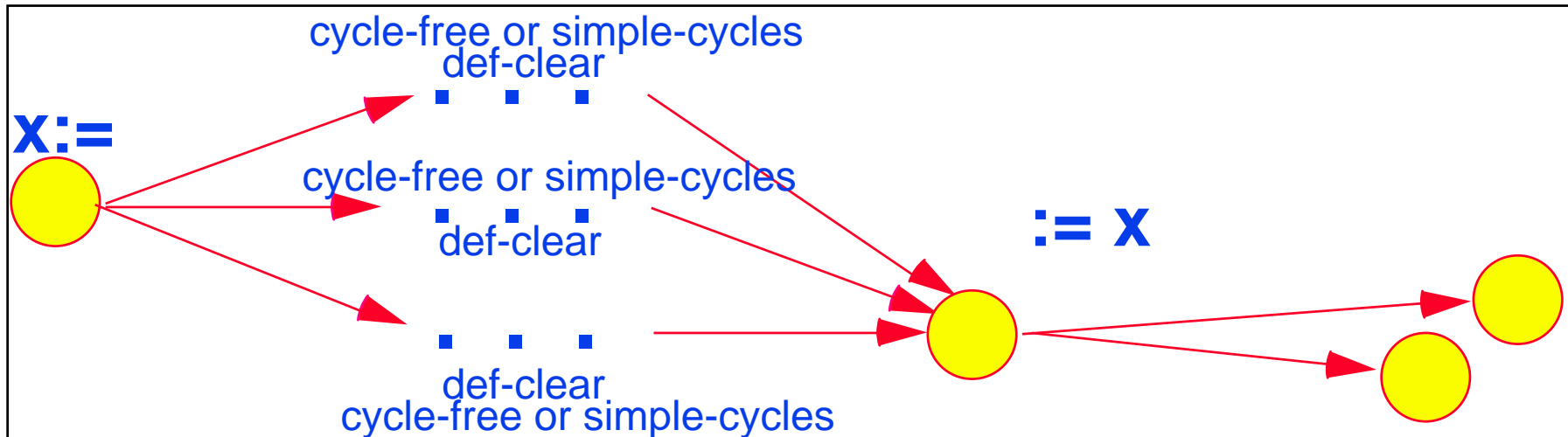
## All-P-Uses, Some-C-Uses

- either All-P-Uses for  $d_m(x)$  or at least one C-Use

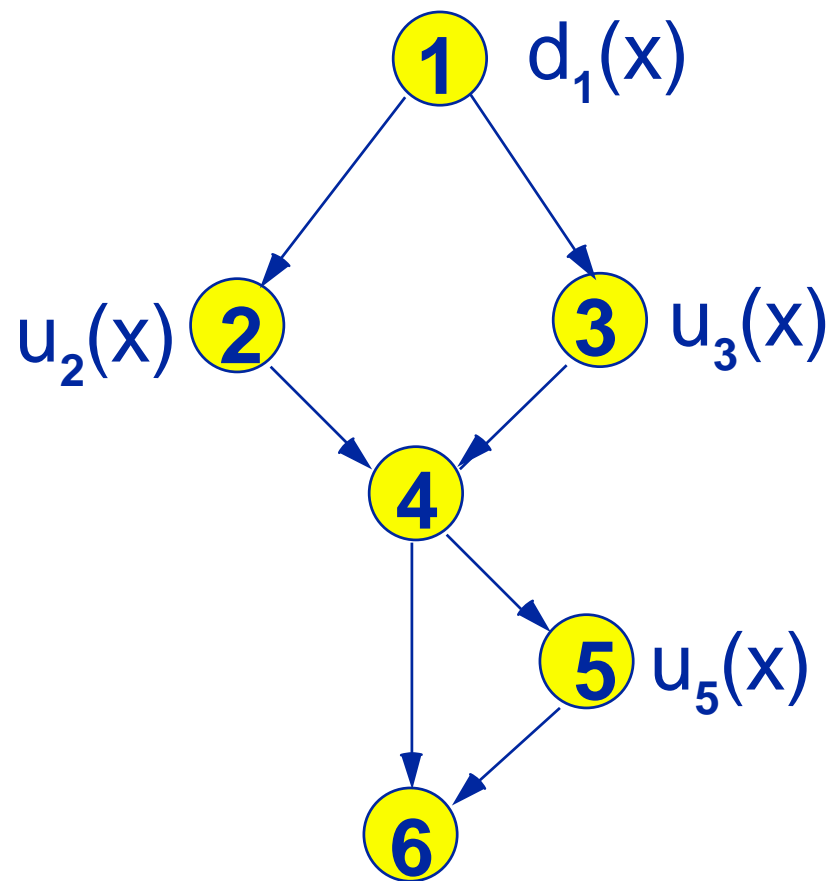
# Rapps' and Weyuker's Data Flow Criteria

## All-Du-Paths

- All definition-clear subpaths that are cycle-free or simple-cycles from **each definition to each use** reached by that definition and each successor node of the use



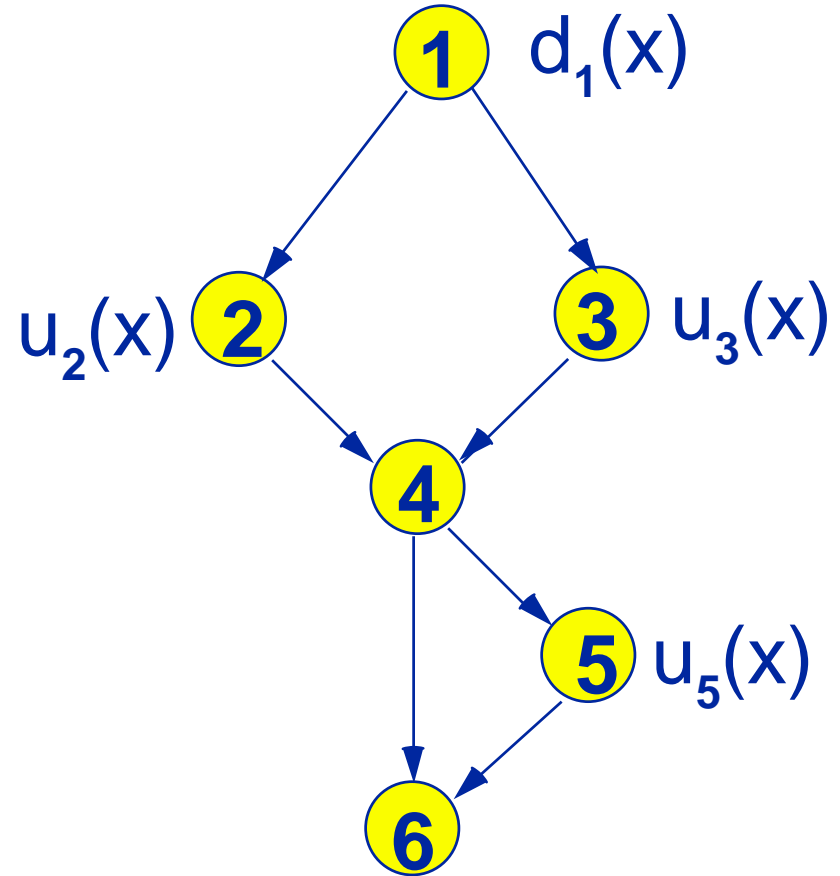
# Example



## All-Defs

Requires:

$d_1(x)$  to a use  
Satisfactory Path:  
1, 2, 4, 6



# All-Uses

Requires:

$d_1(x)$  to  $u_2(x)$

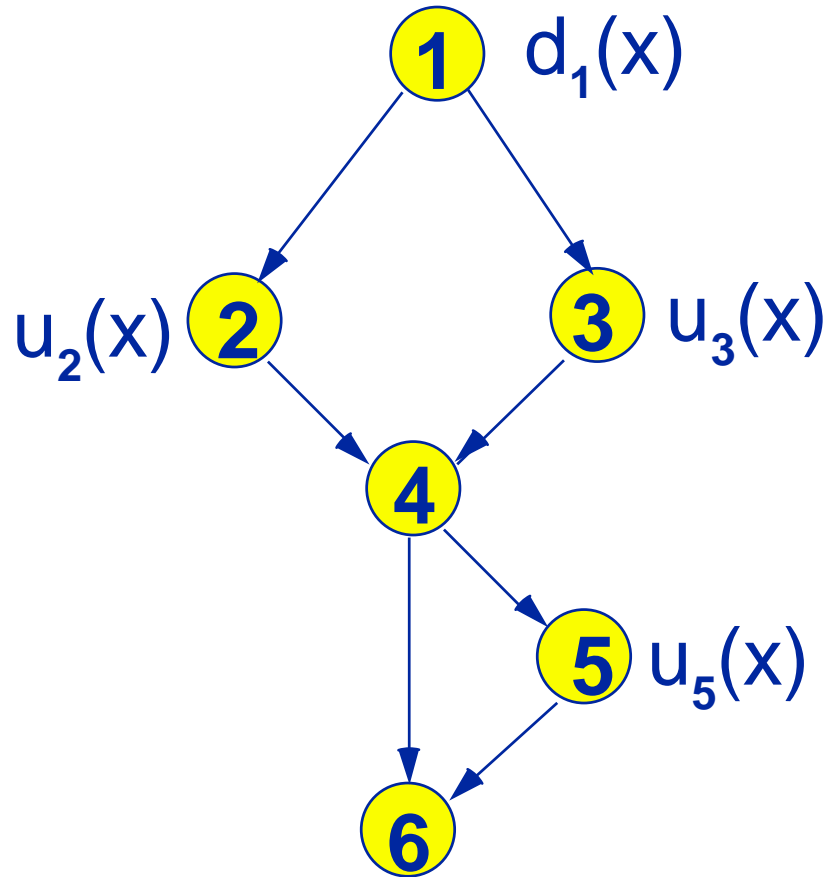
$d_1(x)$  to  $u_3(x)$

$d_1(x)$  to  $u_5(x)$

Satisfactory Paths:

1, 2, 4, 5, 6

1, 3, 4, 6





# All-Du-Paths

Requires:

$d_1(x)$  to  $u_2(x)$

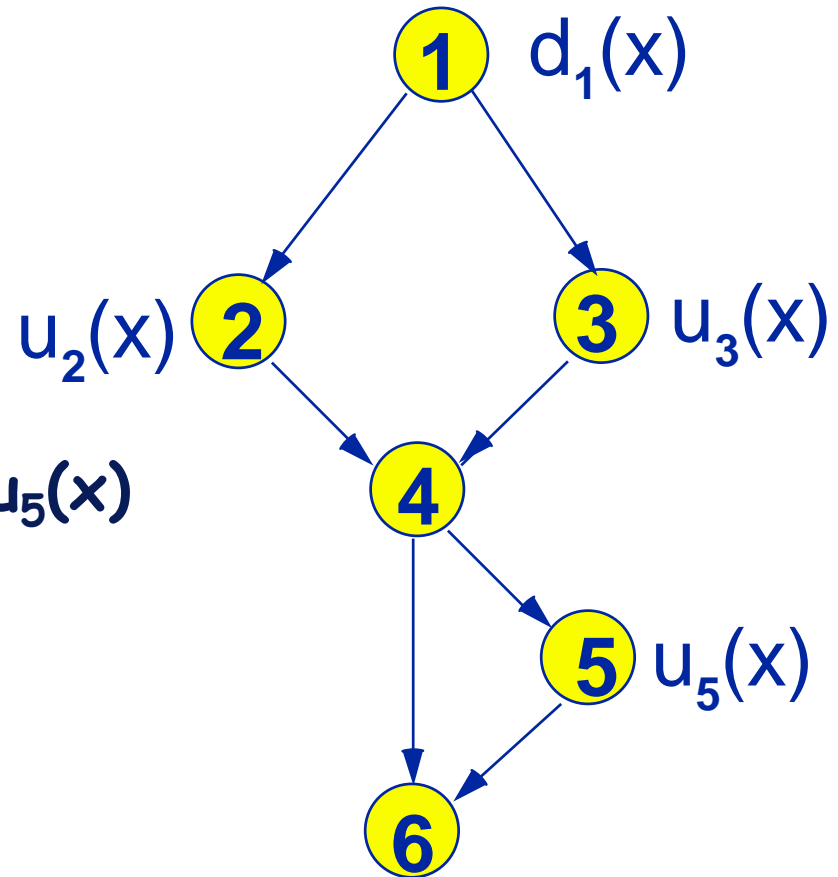
$d_1(x)$  to  $u_3(x)$

both paths for  $d_1(x)$  to  $u_5(x)$

Satisfactory Paths:

1, 2, 4, 5, 6

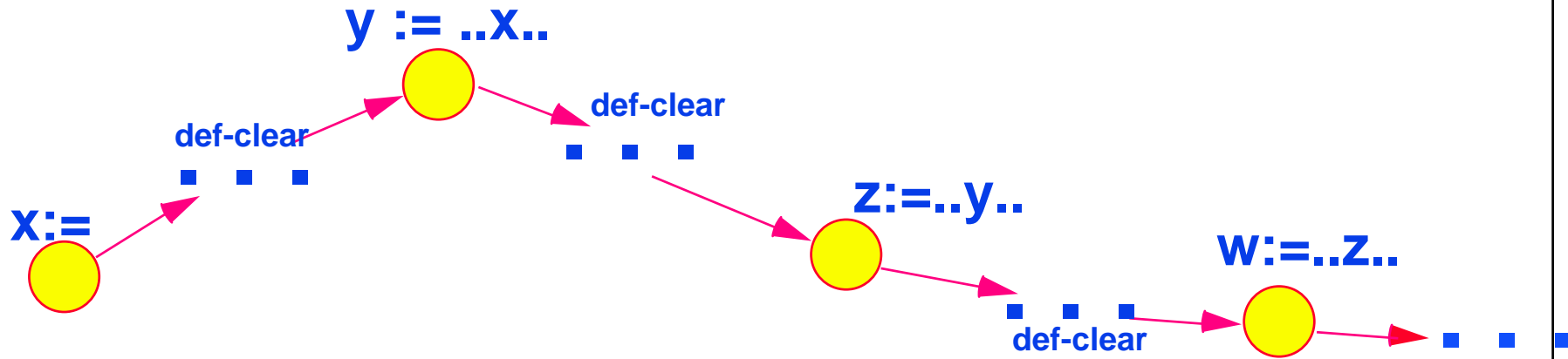
1, 3, 4, 5, 6



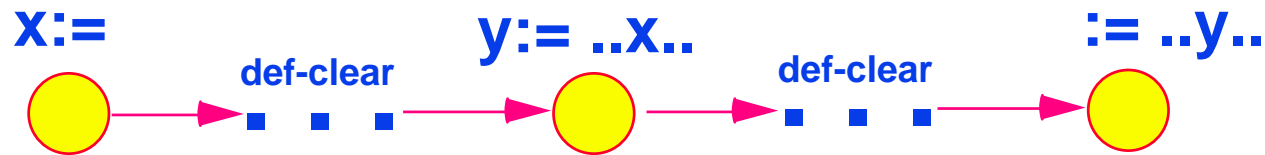
# Ntafos' Data Flow Criteria

- **Foundation:**
  - Chains of alternating definitions and uses linked by definition-clear subpaths (k-dr interactions)
  - $i^{\text{th}}$  definition reaches  $i^{\text{th}}$  use,
  - which defines  $i^{\text{th}+1}$  definition
  - K is number of branches

# k-dr interactions



1-dr



2-dr

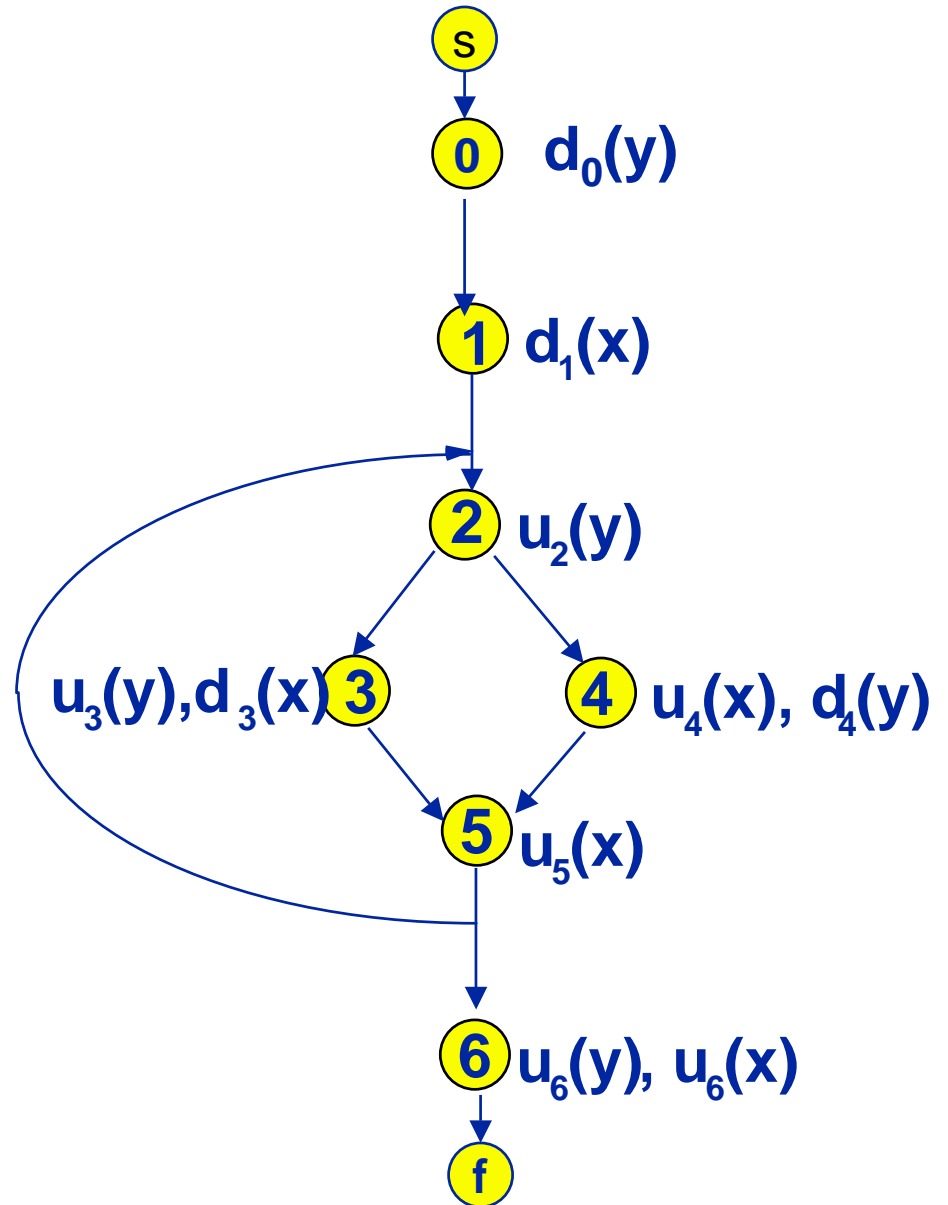
# Ntafos' Data Flow Criteria

- **Required K-tuples**

Some subpath propagating each k-dr interaction

- + if last use is a predicate, both branches
- + if first definition or last use is in a loop, minimal and some larger number of loop iterations

# Example



# 1-DR interaction

a: d1(x) to u4(x)

b: d1(x) to u5(x)

c: d1(x) to u6(x)

d: d0(y) to u2(y)

e: d0(y) to u3(y)

f: d0(y) to u6(y)

g: d3(x) to u5(x)

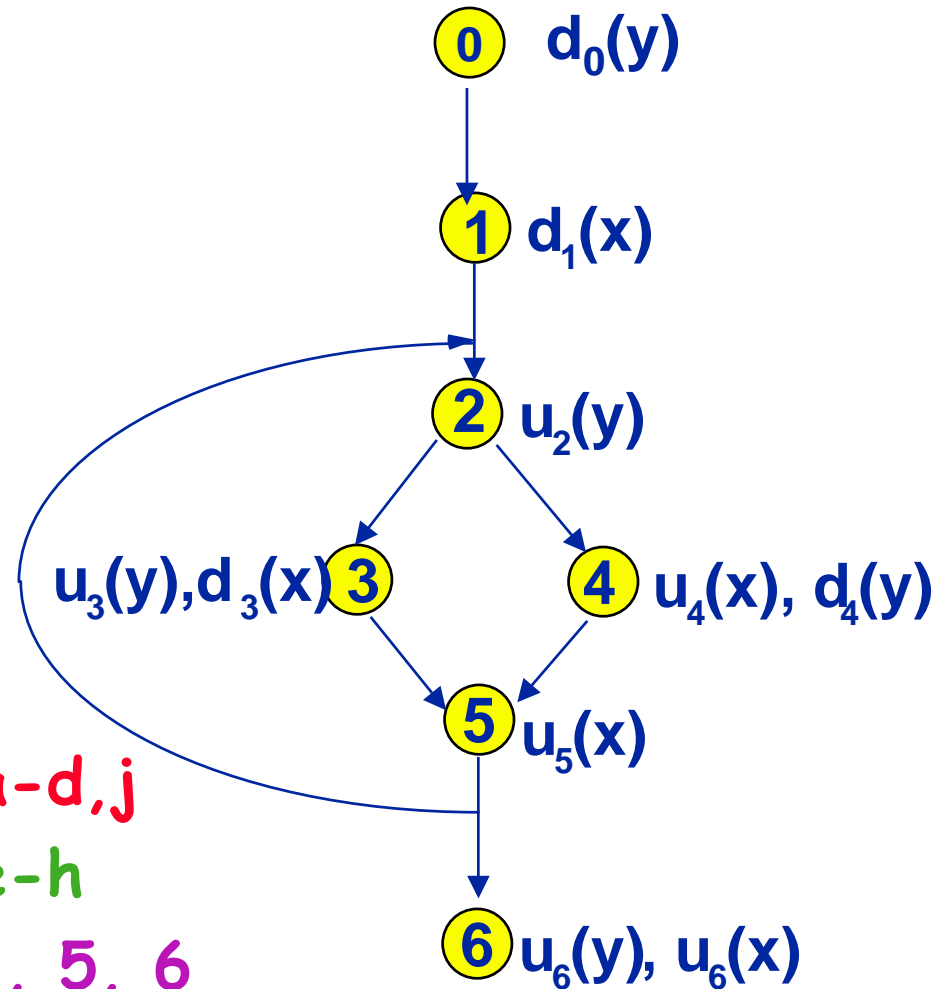
h: d3(x) to u6(x)

i: d3(x) to u4(x)

j: d4(y) to u6(y)

k: d4(y) to u2(y)

l: d4(y) to u3(y)



## PATHS

0, 1, 2, 4, 5, 6: satisfies a-d, j

0, 1, 2, 3, 5, 6: satisfies e-h

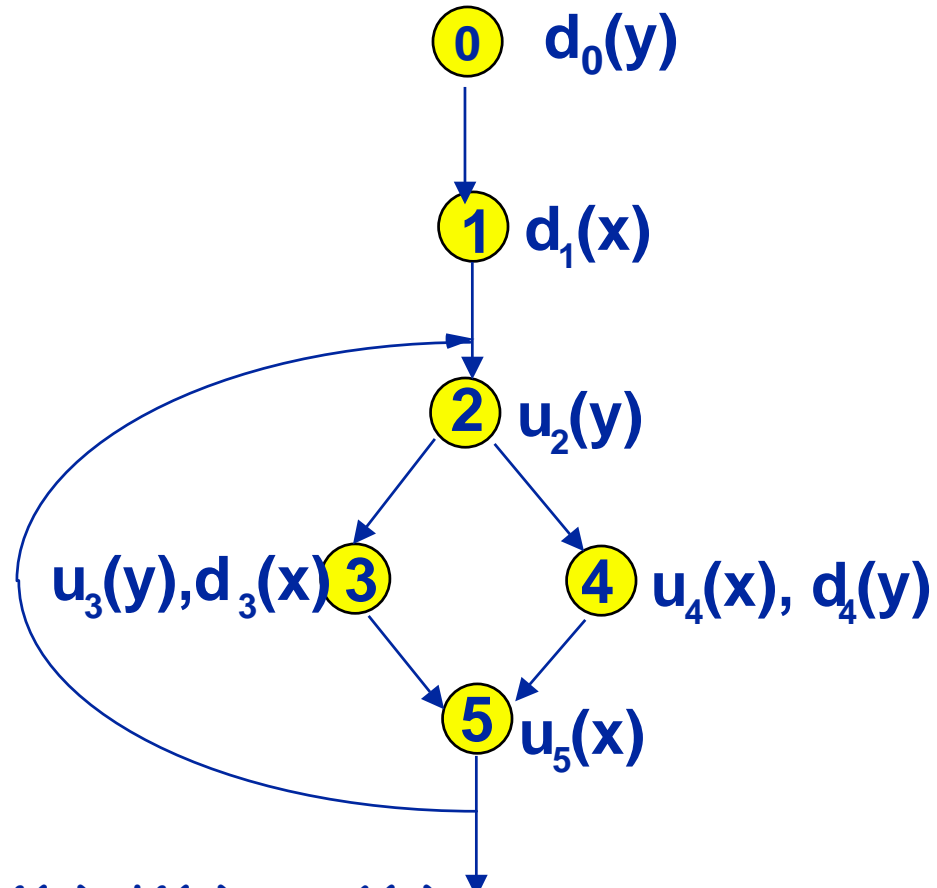
0, 1, 2, 3, 5, 2, 4, 5, 2, 3, 5, 6

: satisfies i, k, l

# From 1-DR to 2-DR

- a: d1(x) to u4(x)
- b: d1(x) to u5(x)
- c: d1(x) to u6(x)
- d: d0(y) to u2(y)
- d: d0(y) to u3(y)
- e: d0(y) to u6(y)
- f:

- g: d3(x) to u5(x)
- h: d3(x) to u6(x)
- i: d3(x) to u4(x)
- j: d4(y) to u6(y)
- j: d4(y) to u2(y)
- k: d4(y) to u3(y)
- l:



Plus:

- d1(x) to u4(x) d4(y) to u6(y)
- d1(x) to u4(x) d4(y) to u2(y)
- d1(x) to u4(x) d4(y) to u3(y)
- d0(y) to u3(y) d3(x) to u5(x)
- d0(y) to u3(y) d3(x) to u6(x)
- d0(y) to u3(y) d3(x) to u4(x)

- d3(x) to u4(x) d4(y) to u6(y)
- d3(x) to u4(x) d4(y) to u2(y)
- d3(x) to u4(x) d4(y) to u3(y)
- d4(y) to u3(y) d3(x) to u5(x)
- d4(y) to u3(y) d3(x) to u6(x)
- d4(y) to u3(y) d3(x) to u4(x)

## 2-DR interactions

**aj:** d1(x), u4(x), d4(y), u6(y)

**ak:** d1(x), u4(x), d4(y), u2(y)

**al:** d1(x), u4(x), d4(y), u3(y)

**eg:** d0(y), u3(y), d3(x), u5(x)

**eh:** d0(y), u3(y), d3(x), u6(x)

**ei:** d0(y), u3(y), d3(x), u4(x)

**ij:** d3(x), u4(x), d4(y), u6(y)

**ik:** d3(x), u4(x), d4(y), u2(y)

**il:** d3(x), u4(x), d4(y), u3(y)

**lg:** d4(y), u3(y), d3(x), u5(x)

**lh:** d4(y), u3(y), d3(x), u6(x)

**li:** d4(y), u3(y), d3(x), u4(x)

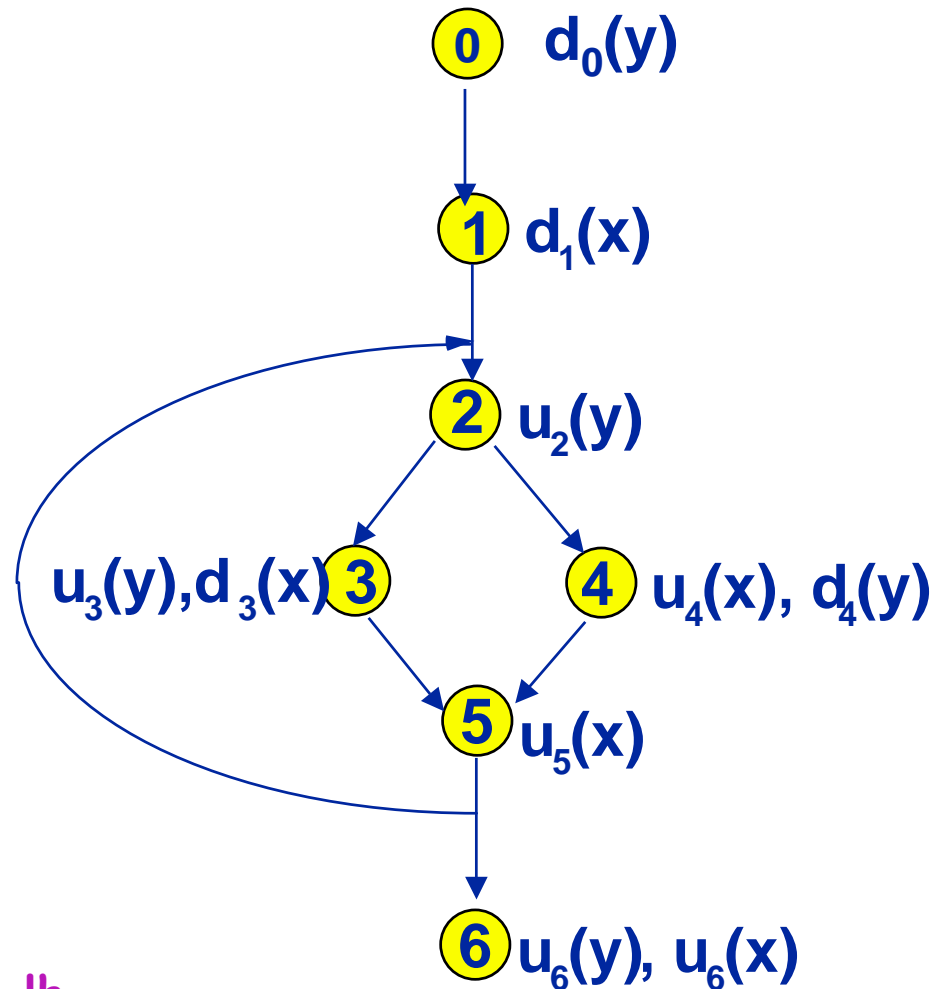
**Paths:**

**0, 1, 2, 4, 5, 6: satisfies aj**

**0, 1, 2, 3, 5, 6: satisfies eg, eh**

**0, 1, 2, 3, 5, 2, 4, 5, 2, 3, 5, 6**  
: satisfies ei, ij, ik, il, lh

**0, 1, 2, 4, 5, 2, 3, 5, 6: satisfies ak, al, lg (but not li)**





# Laski's and Korel's Criteria

- **Foundation:**

Combinations of definitions that reach uses at some node via a subpath

- **Reach Coverage**

Some definition-clear subpath from each definition to all uses reached by that definition

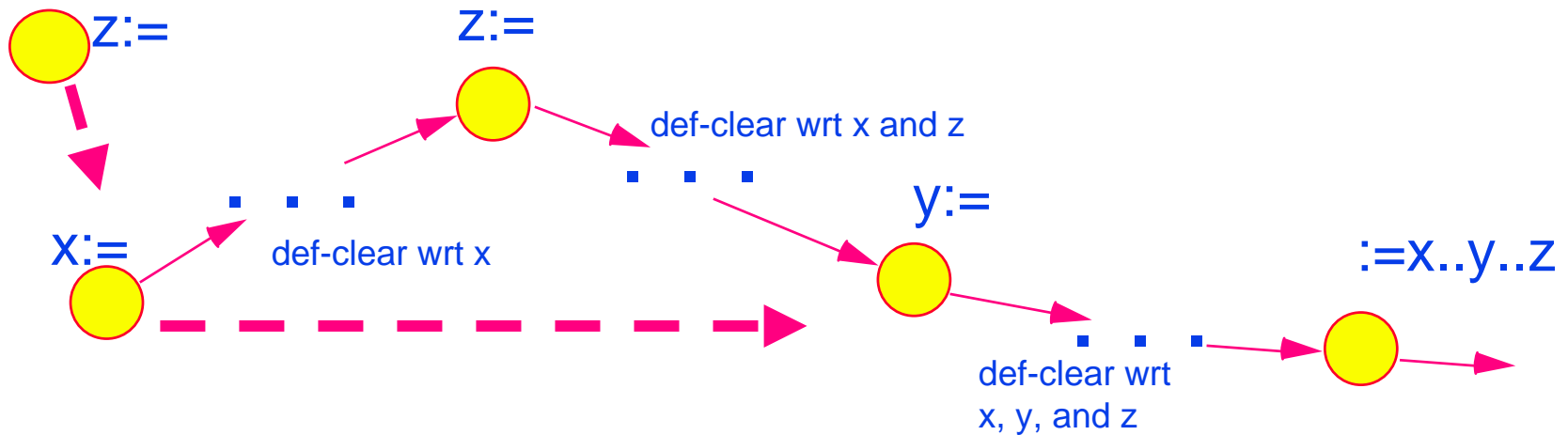
basically the same as all-uses

# Laski's and Korel's Criteria

- **Context Coverage**

Some subpath along which each **set** of definitions reach uses at each node

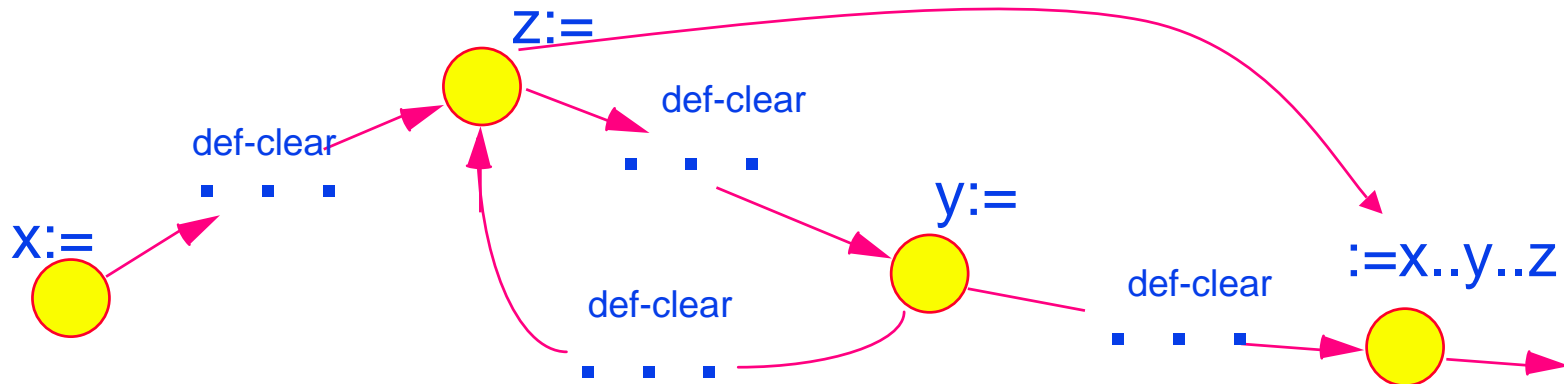
$:=X..y..Z$



# Laski's and Korel's Criteria

- Ordered Context Coverage

Some subpath along which each **sequence** of definitions reach uses at each node



# Context Coverage

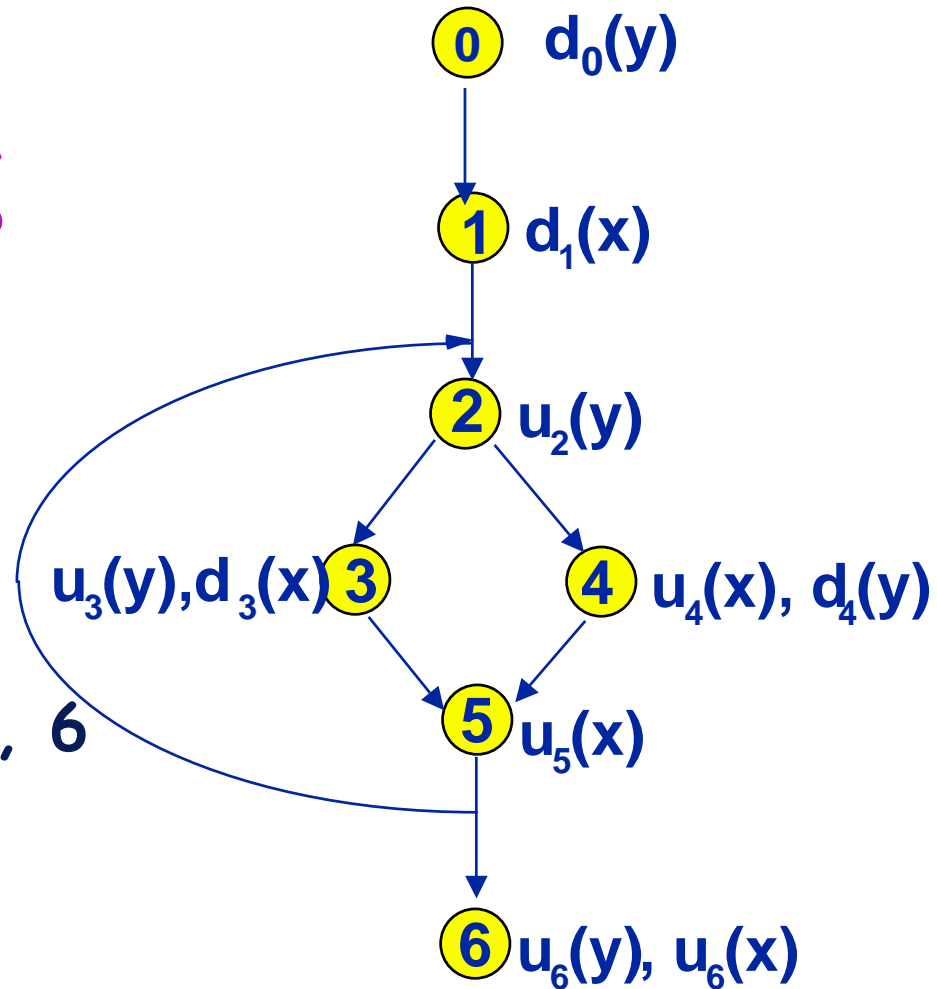
$$DC(n_6) = \begin{array}{l} \{d_1(x), d_4(y)\}, \\ \{d_3(x), d_0(y)\}, \\ \{d_3(x), d_4(y)\} \end{array} \begin{array}{l} a \\ b \\ c \end{array}$$

## Paths

a: 1, 2, 4, 5, 6

b: 1, 2, 3, 5, 6

c: 1, 2, 3, 5, 2, 4, 5, 6



Note: must compute the sets for each node

# Ordered Context Coverage

$$\text{ODC}(n_6) = \begin{array}{ll} [d_1(x), d_4(y)], & a \\ [d_0(y), d_3(x)], & b \\ [d_3(x), d_4(y)], & c \\ [d_4(y), d_3(x)], & d \end{array}$$

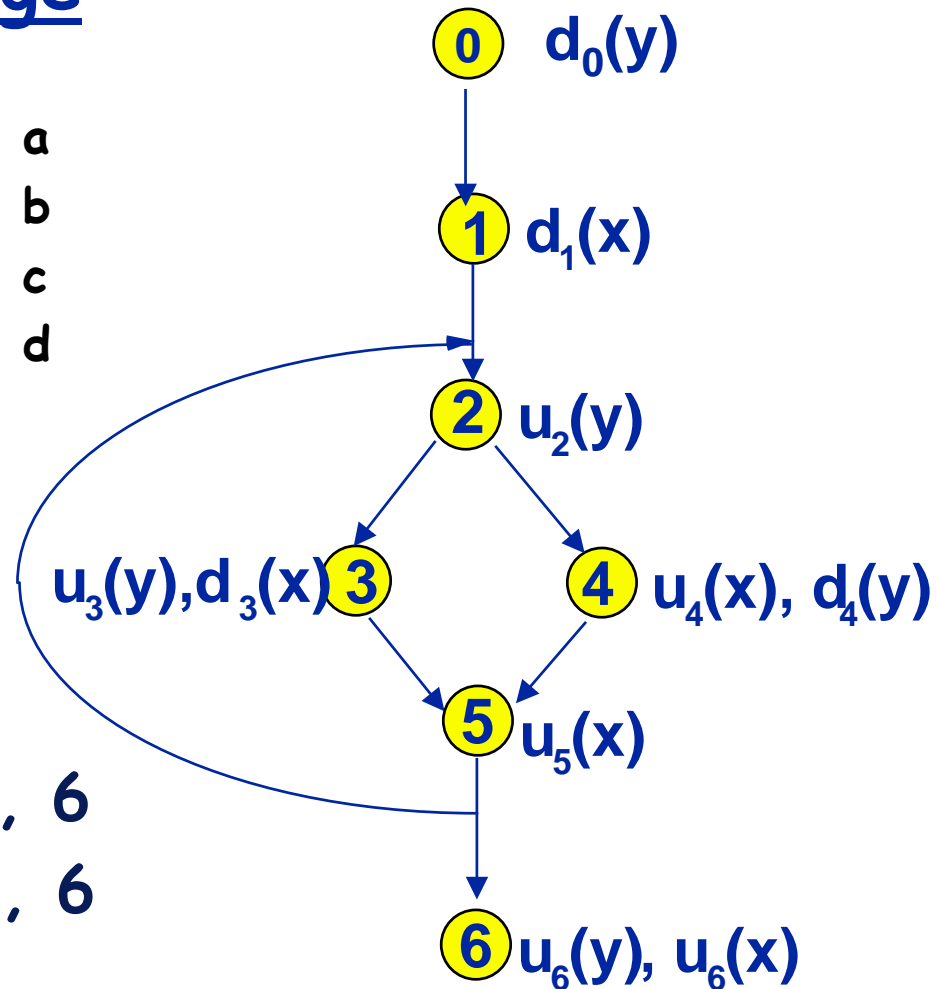
## Paths

a: 1, 2, 4, 5, 6

b: 1, 2, 3, 5, 6

c: 1, 2, 3, 5, 2, 4, 5, 6

d: 1, 2, 4, 5, 2, 3, 5, 6



Note: must compute the sequences for each node

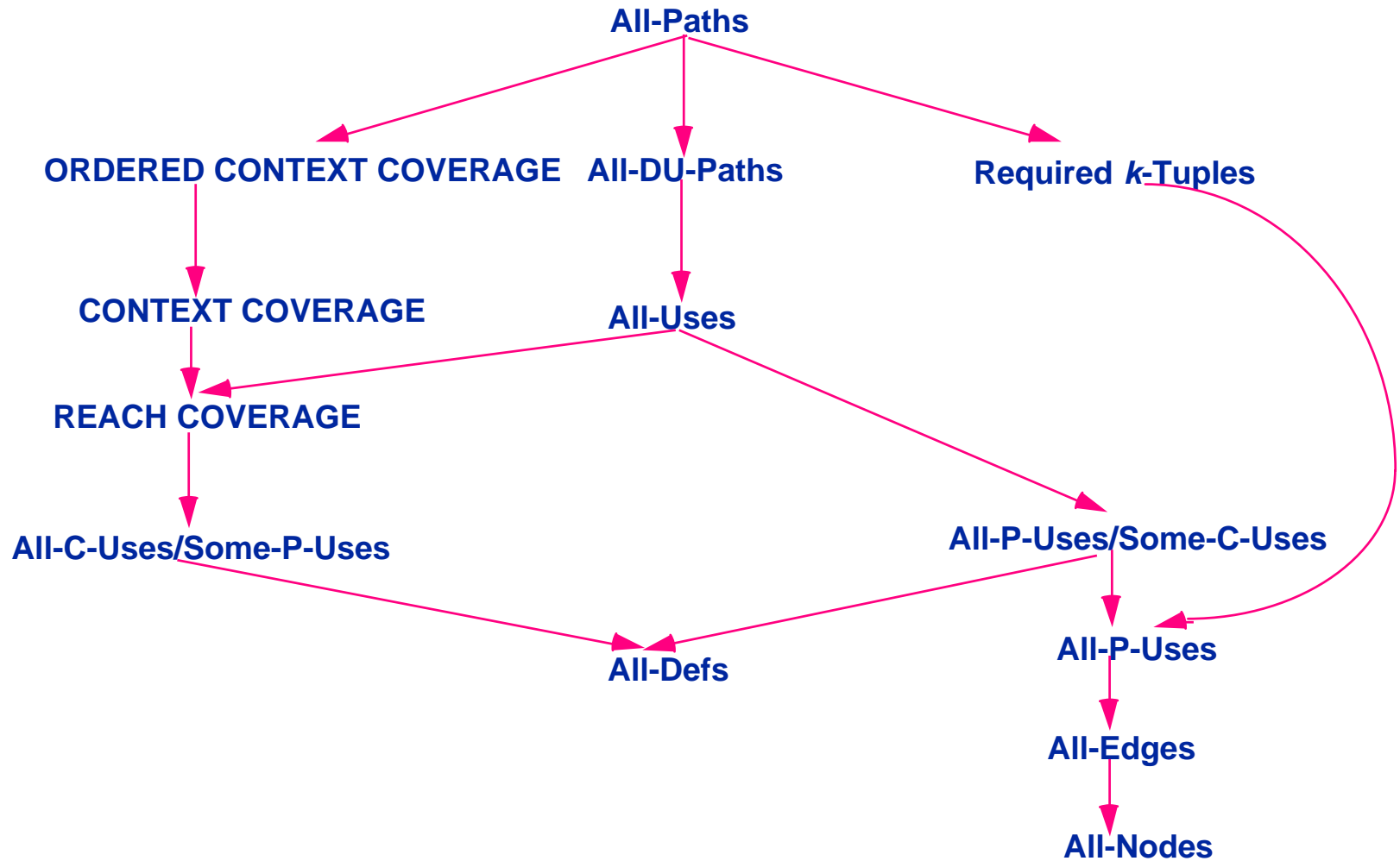
## How can we compare these criteria?

- all select a set of paths, so compare the paths that they select
  - set of paths that satisfy a criterion are not necessarily unique
  - e.g.,  $s_1$  or  $s_2$  satisfies criterion A
  - $s_1$ ,  $s_2$ , or  $s_3$  satisfy criterion B

## How can we compare these criteria?

- define a subsumption relationship
- criterion A subsumes criterion B iff for any flow graph  
$$P \text{ satisfies } A \implies P \text{ satisfies } B$$
- criterion A is equivalent to criterion B iff A subsumes B and B subsumes A

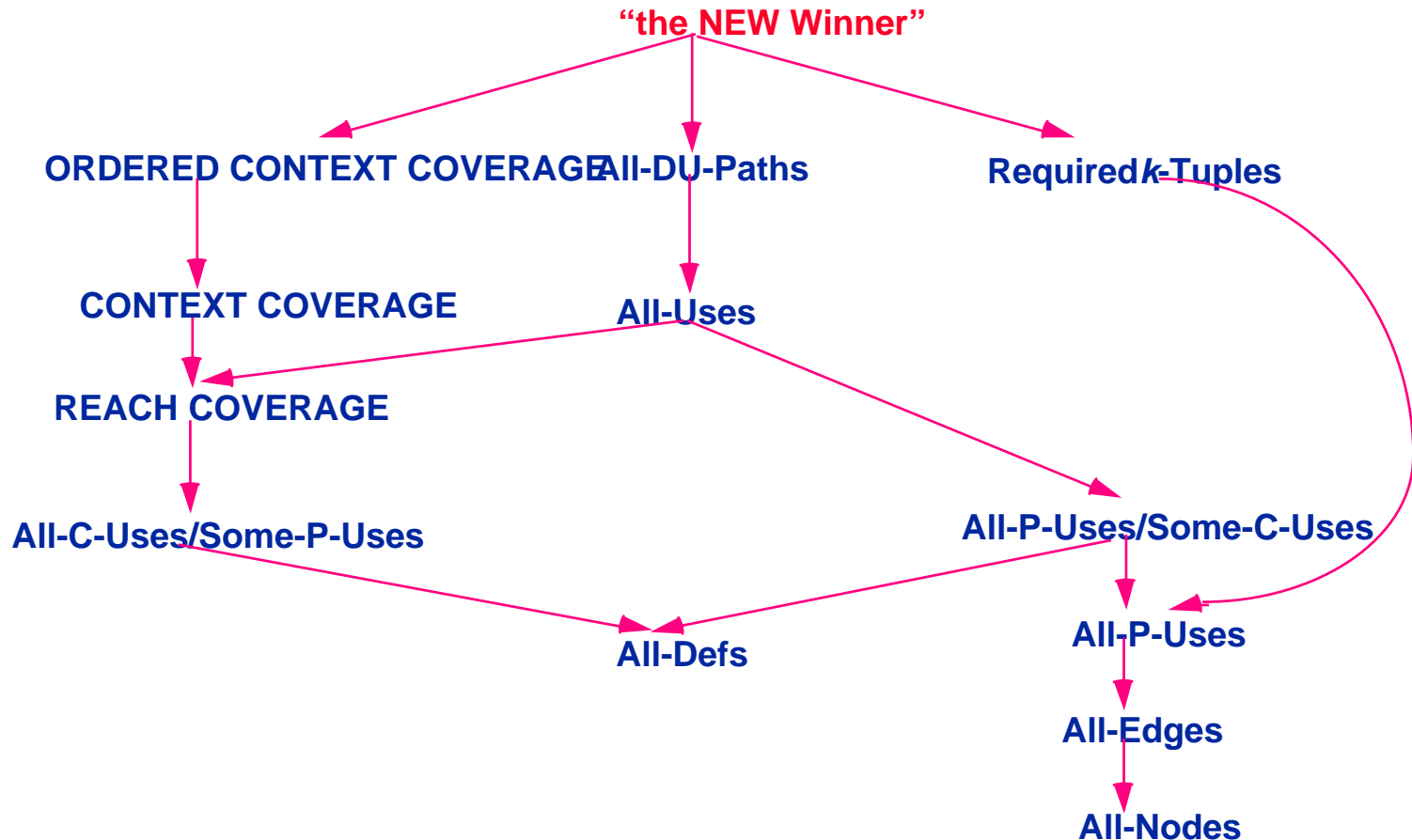
# Relationships among these criteria





# Should we define yet another criteria?

- could subsume all the others, (except all paths)?



## Problems with data flow coverage criteria

- infeasible paths
  - Don't usually get 100% coverage
- Need to understand fault detection ability
- Artificially combines control with data flow
  - Considering p-uses or all predicate alternatives, tacked on to incorporate control flow

## Conclusions

- An improvement over control flow techniques
- Provides a rationale for how many times to iterate a loop or which combinations of subpaths to consider
- Most commonly used criterion is all-uses
- Need more empirical evidence to evaluate effectiveness