

# Fault-based Testing

## Reading assignment

- JUnit is a regression testing framework written by Erich Gamma and Kent Beck.
- JUnit Test Infected: Programmers Love Writing Tests ,  
<http://junit.sourceforge.net/doc/testinfected/testing.htm>
- References
  - JUnit, <http://junit.sourceforge.net/>
  - <http://www.junit.org/index.htm>

# Structural Test Data Selection

- Random
  - Coverage based
    - Control flow
    - Data flow
  - Fault-based
    - Error (fault) seeding
      - e.g., mutation testing
    - Fault constraints
      - E.g., RELAY
  - Error-based (Failure-based)
    - domain and computation based
      - use representations created by symbolic execution
- } Dependence based analysis

# Fault Based Techniques

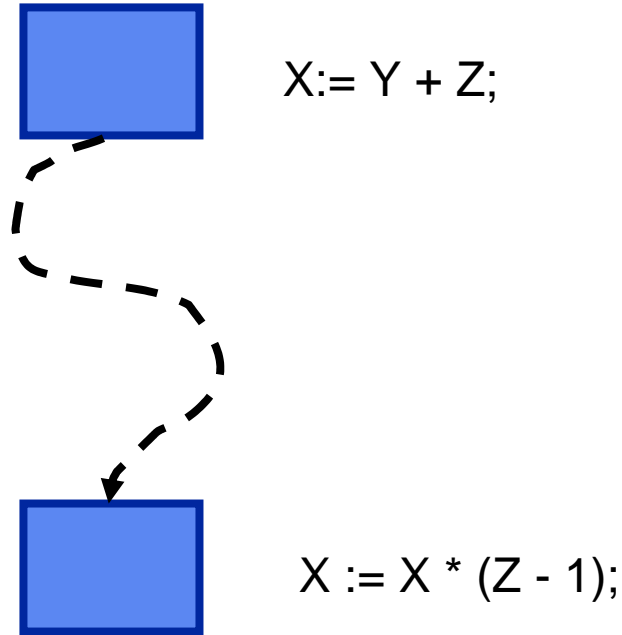
- For each statement try to select test data that will expose faults at that statement
  - Mutation testing monitors effectiveness
  - Fault constraints --instead of monitoring if the selected test data kills a mutant, determine the **necessary conditions** to guarantee that the fault is revealed if it exists

## Remember: comments on dependence based testing coverage

- for selecting test cases
  - syntactic dependence alone is not adequate
    - the number of syntactic dependencies in a program can be quadratic in the number of statements
    - a given syntactic dependence may be demonstrated by (infinitely) many paths
    - propagation of a fault through a particular path may depend on the selection of input data  
⇒ must use semantic information

Can we do better than this?????

# Can exercise a dependence relationship but not reveal the fault



## Relay Model

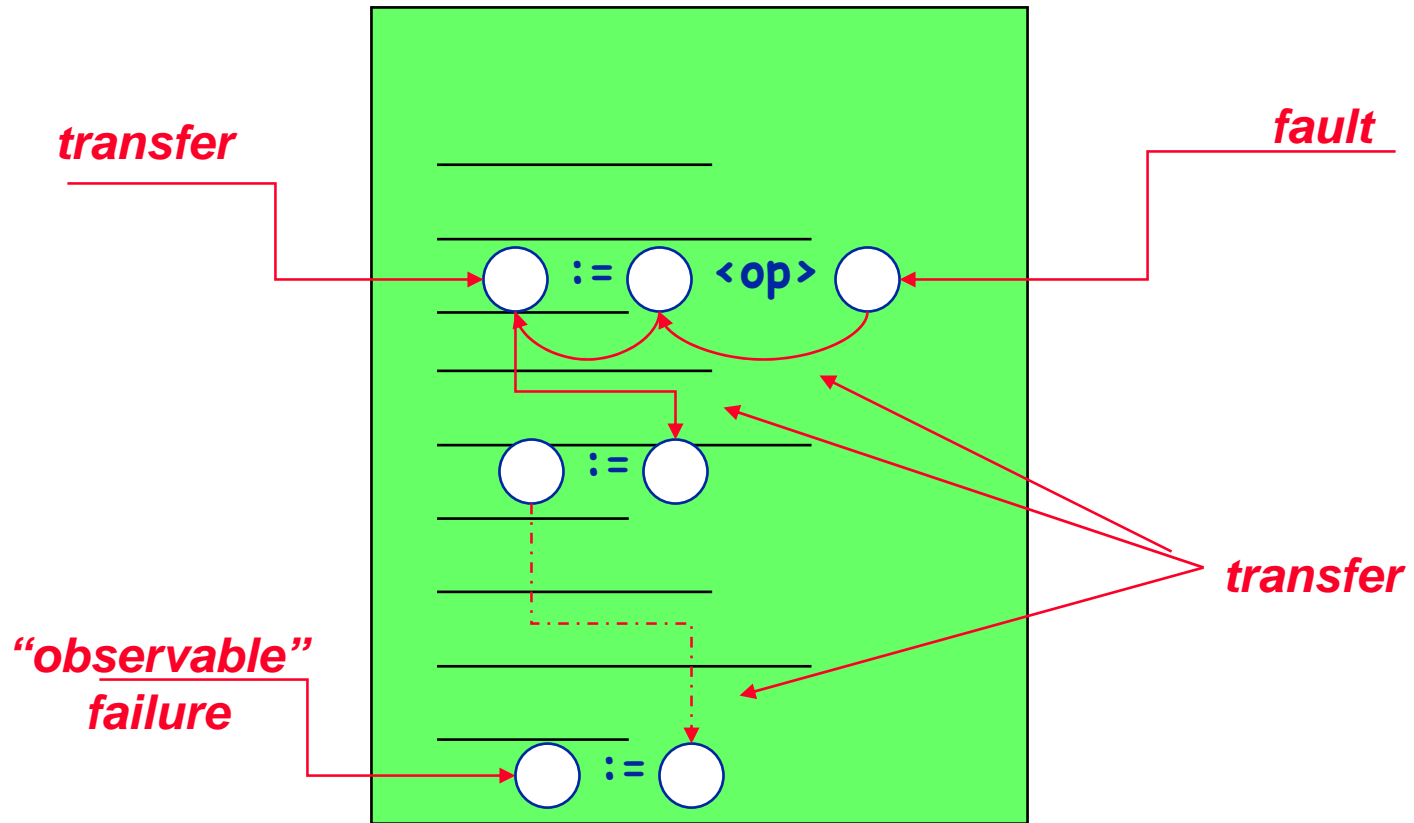
- **Selective semantic information + syntactic dependency information**
  - origination of a fault
  - computational transfer of a fault
  - propagation of a fault (based on data and control flow)
- Define necessary and sufficient conditions for detecting certain classes of faults

# Overview of Relay Model

- origination
  - introduction of potential failure at smallest (valued) subexpression containing fault
- transfer
  - “movement” of potential failure in program
    - Within the originating statement
      - computational transfer
    - From one statement to the next
      - data dependence transfer
      - control dependence transfer



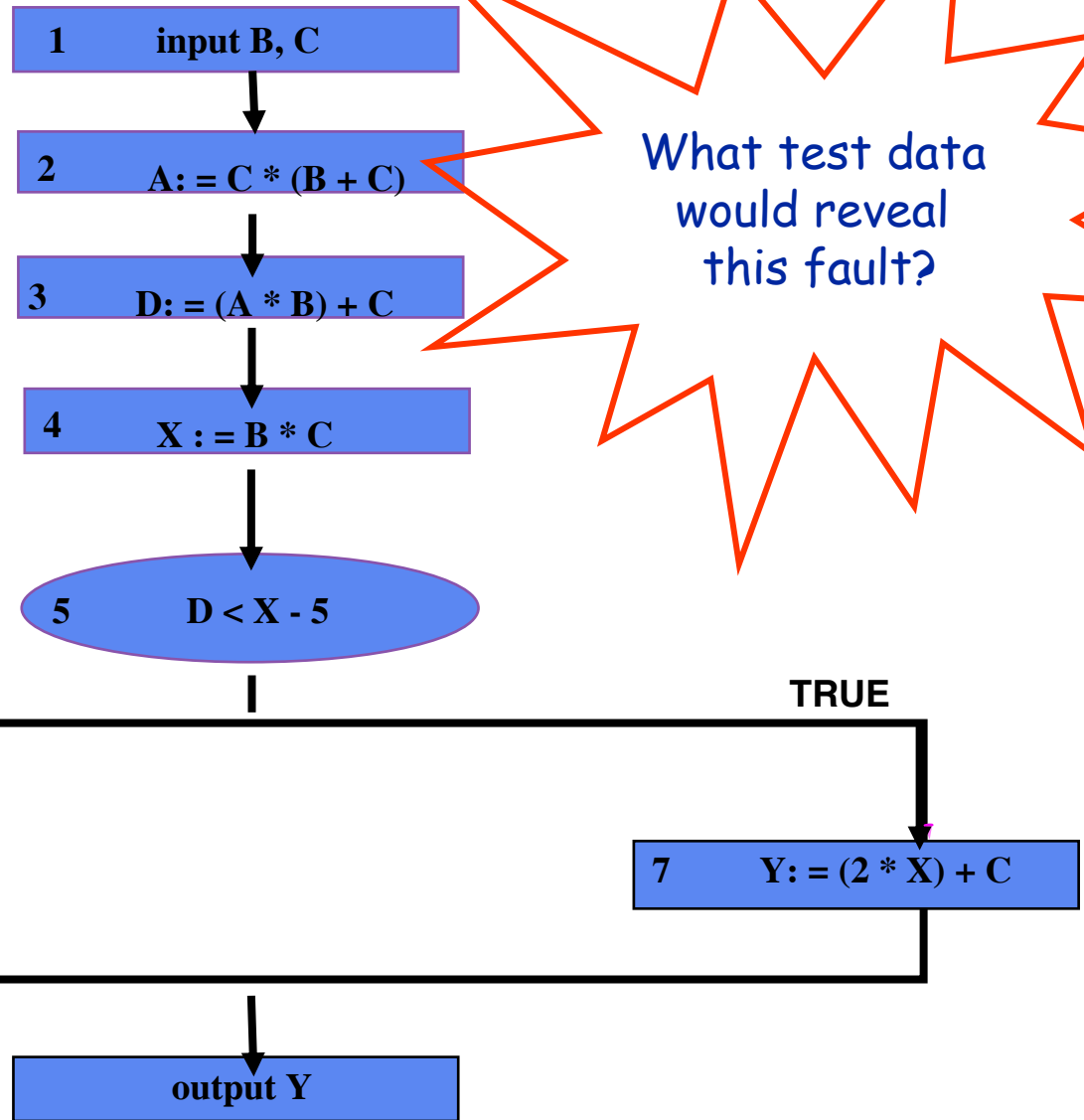
# Relay Model



# Example

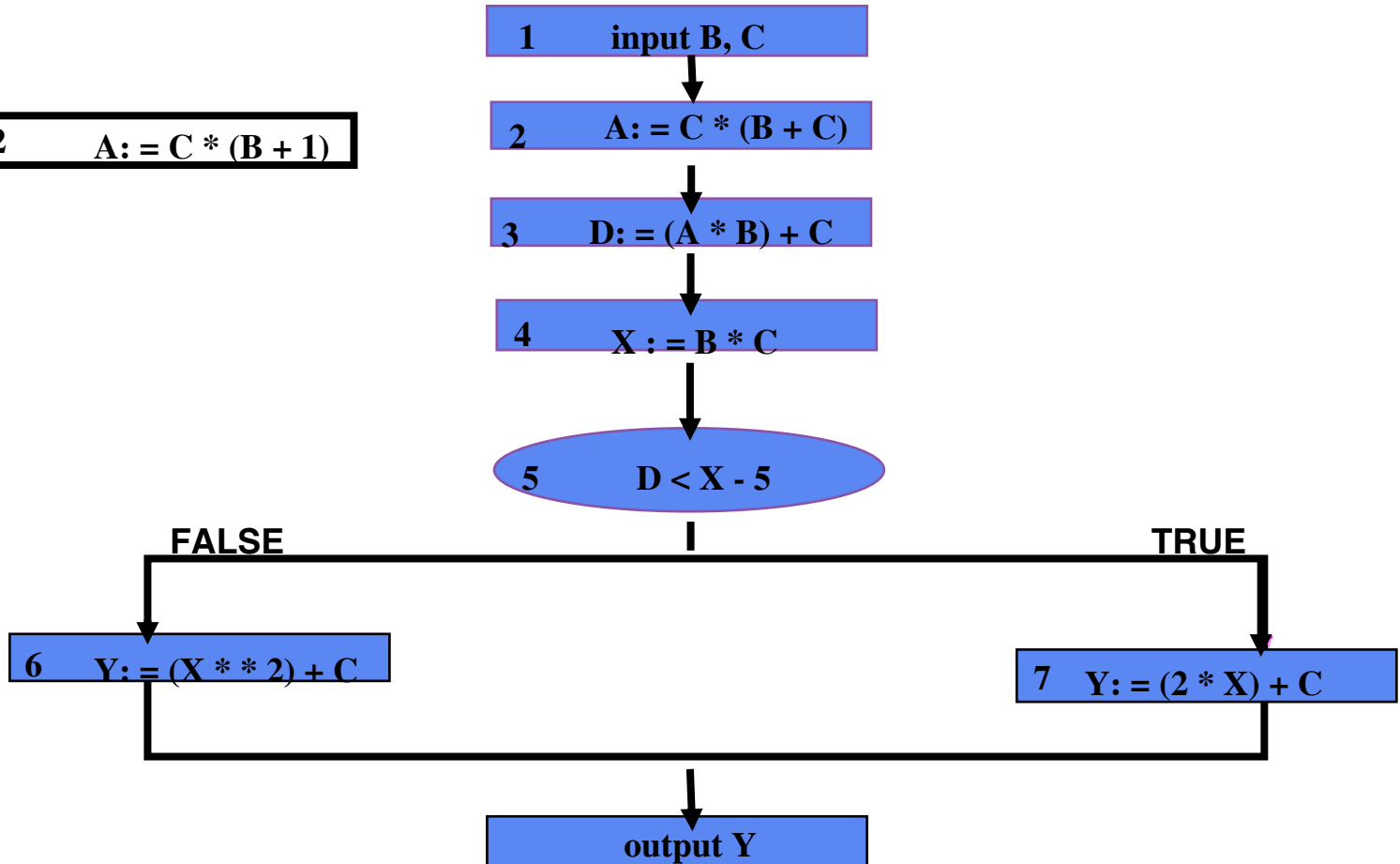
Correct:

2  $A := C * (B + 1)$



# Example

2     $A := C * (B + 1)$

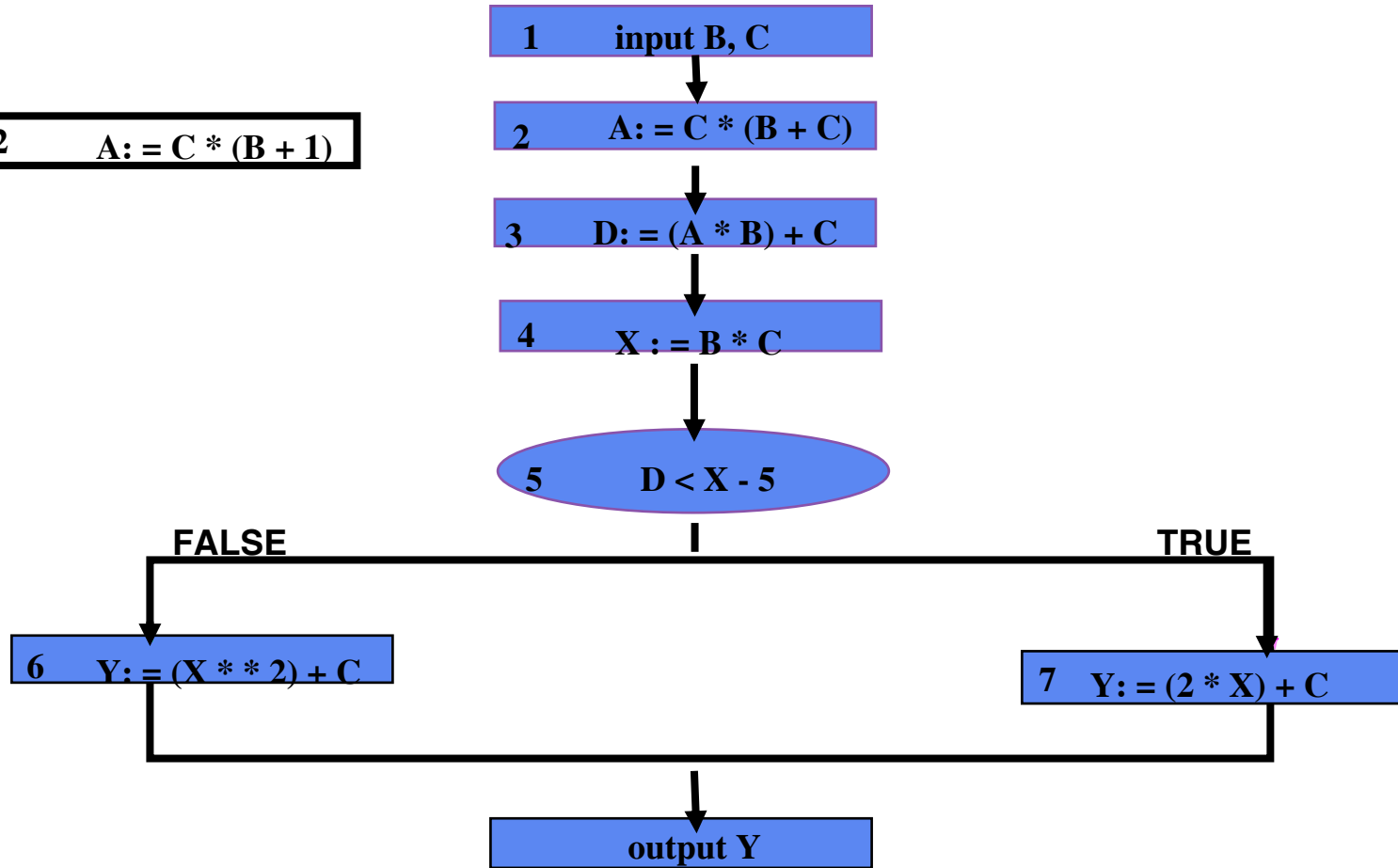


	module	t. c.		exp	a	d	x	d < x - 5	y	output
		b	c							
B+C	faulty	1	1	2	2	3	1	F	2	2
B+1	correct	1	1	2	2	3	1	F	2	2

NO ORIGINATION OF POTENTIAL FAILURE AT NODE 2

# Example

2  $A := C * (B + 1)$

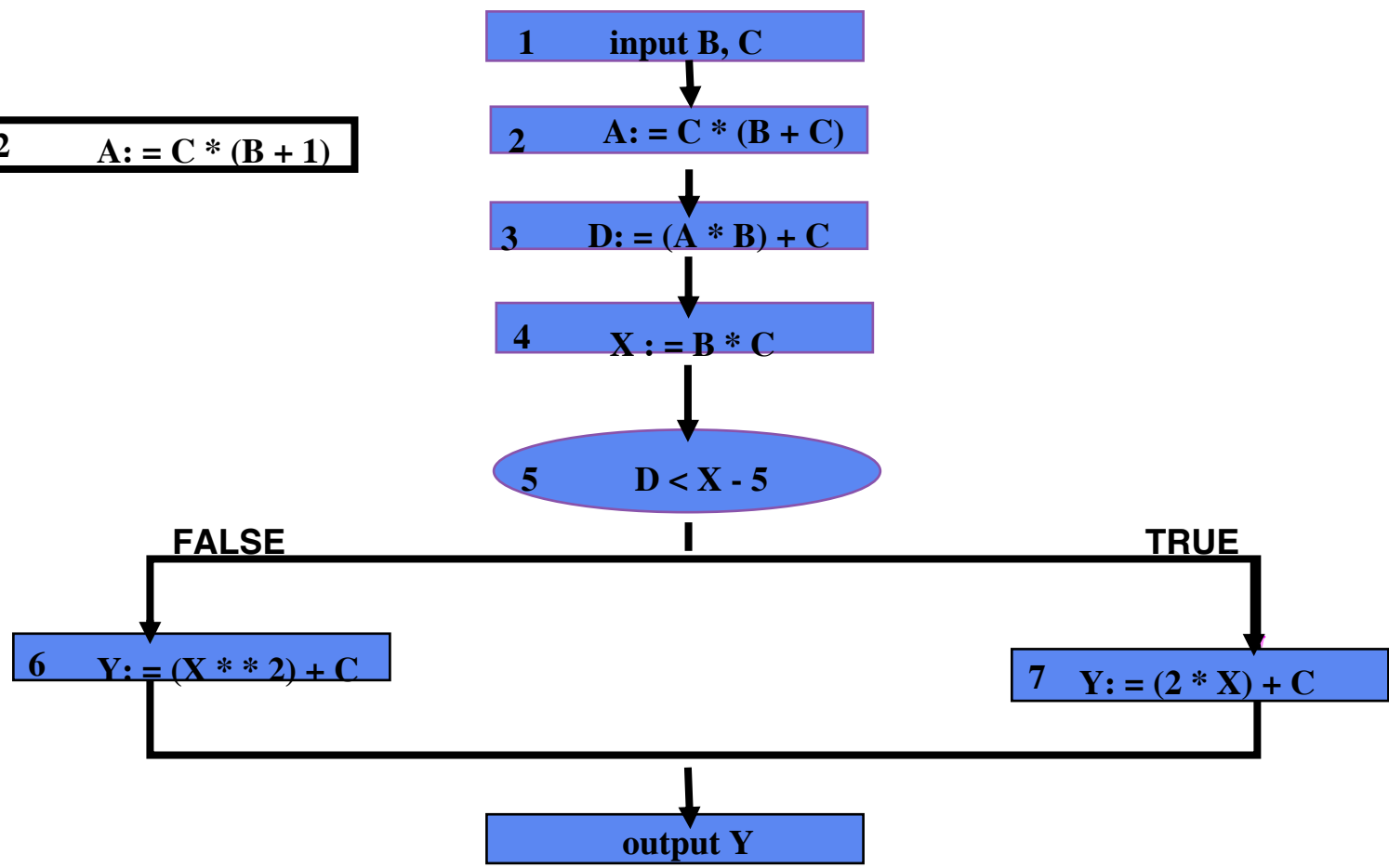


	module	t. c.		exp	a	d	x	$d < x - 5$	y	output
		b	c							
B+C	faulty	1	0	1	0	0	0	F	0	0
B+1	correct	1	0	2	0	0	0	F	0	0

ORIGINATION (NODE 2),  
NO COMPUTATIONAL TRANSFER AT NODE 2

# Example

2  $A := C * (B + 1)$



	module	t. c.		exp	a	d	x	d < x - 5	y	output
		b	c							
B+C	faulty	0	3	3	9	3	0	F	3	3
B+1	correct	0	3	1	3	3	0	F	3	3

ORIGINATION, COMP. TRANSFER (NODE 2)  
 NO DATA DEPENDENCE TRANSFER AT NODE 3

# Example

2  $A := C * (B + 1)$

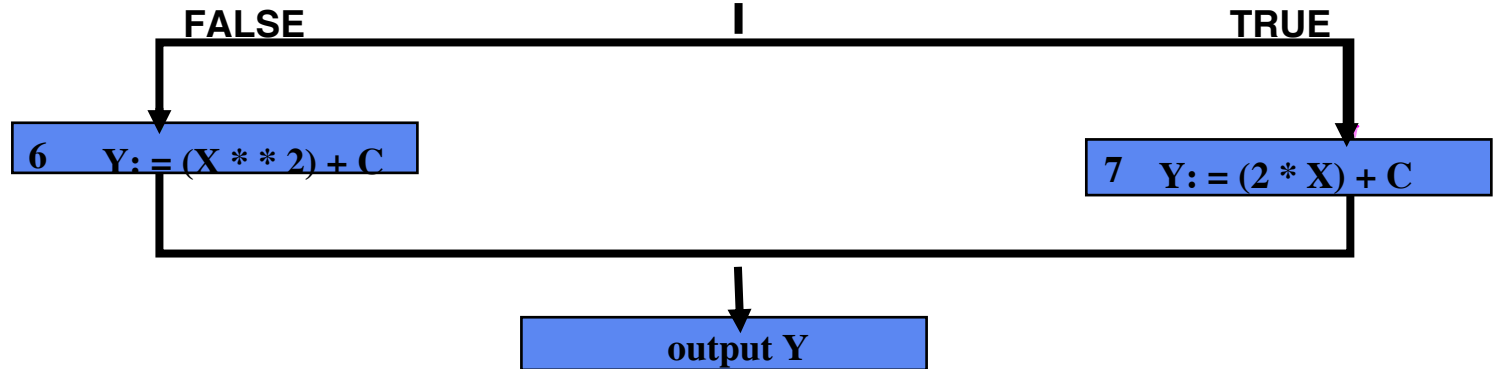
1 input B, C

2  $A := C * (B + C)$

3  $D := (A * B) + C$

4  $X := B * C$

5  $D < X - 5$



	module	t. c.		exp	a	d	x	$d < x - 5$	y	output
		b	c							
B+C	faulty	2	3	5	15	33	6	F	39	39
B+1	correct	2	3	3	9	21	6	F	39	39

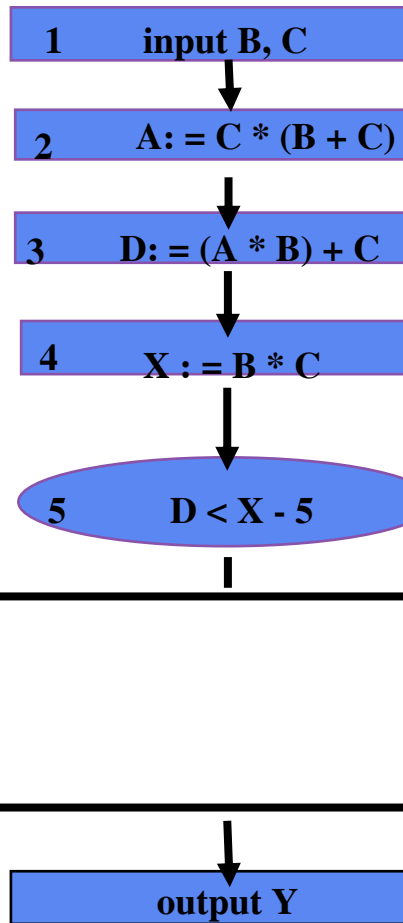
ORIGINATION, COMP. TRANSFER (NODE 2)

DATA DEPENDENCE TRANSFER (NODE 3)

NO DATA DEPENDENCE TRANSFER AT NODE 5

# Example

2  $A := C * (B + 1)$



	module	t. c.		exp	a	d	x	d < x - 5	y	output
		b	c							
B+C	faulty	-2	-1	-3	3	-7	2	T	3	3
B+1	correct	-2	-1	-1	1	-3	2	F	3	3

ORIGINATION, COMP. TRANSFER (NODE 2)

DATA DEPENDENCE TRANSFER (NODES 3, 5)

NO CONTROL DEPENDENCE TRANSFER AT NODE 7 and 6

# Example

2  $A := C * (B + 1)$

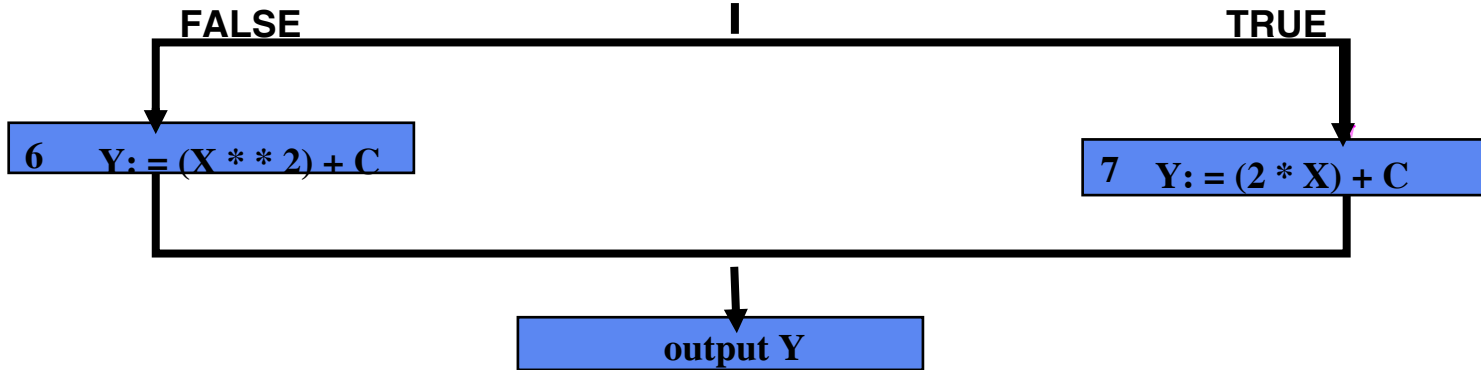
1 input B, C

2  $A := C * (B + C)$

3  $D := (A * B) + C$

4  $X := B * C$

5  $D < X - 5$



	module	t. c.		exp	a	d	x	$d < x - 5$	y	output
		b	c							
B+C	faulty	1	-3	-2	6	3	-3	F	6	6
B+1	correct	1	-3	2	-6	-9	-3	T	-9	-9

ORIGINATION, COMP. TRANSFER (NODE 2)  
 DATA DEPENDENCE TRANSFER (NODES 3, 5)  
 CONTROL DEPENDENCE TRANSFER (NODE 6)  
 FAILURE AT NODE 8



# To Guarantee Detection

**Step 1: guarantee introduction of potential failure at statement containing hypothetical fault**

- origination condition
- computational transfer conditions at statement
- called original state potential failure condition

**Step 2: guarantee transfer of potential failure along information flow to some output**

- called transfer set condition

## Step 1a

- origination condition
  - guarantees introduction of potential failure in smallest subexpression
  - $exp \neq exp^*$
  - defined for fault
  - suppose  $c^*(b+1)$  instead of  $c^*(b+c)$   
 $\Rightarrow c \neq 1$

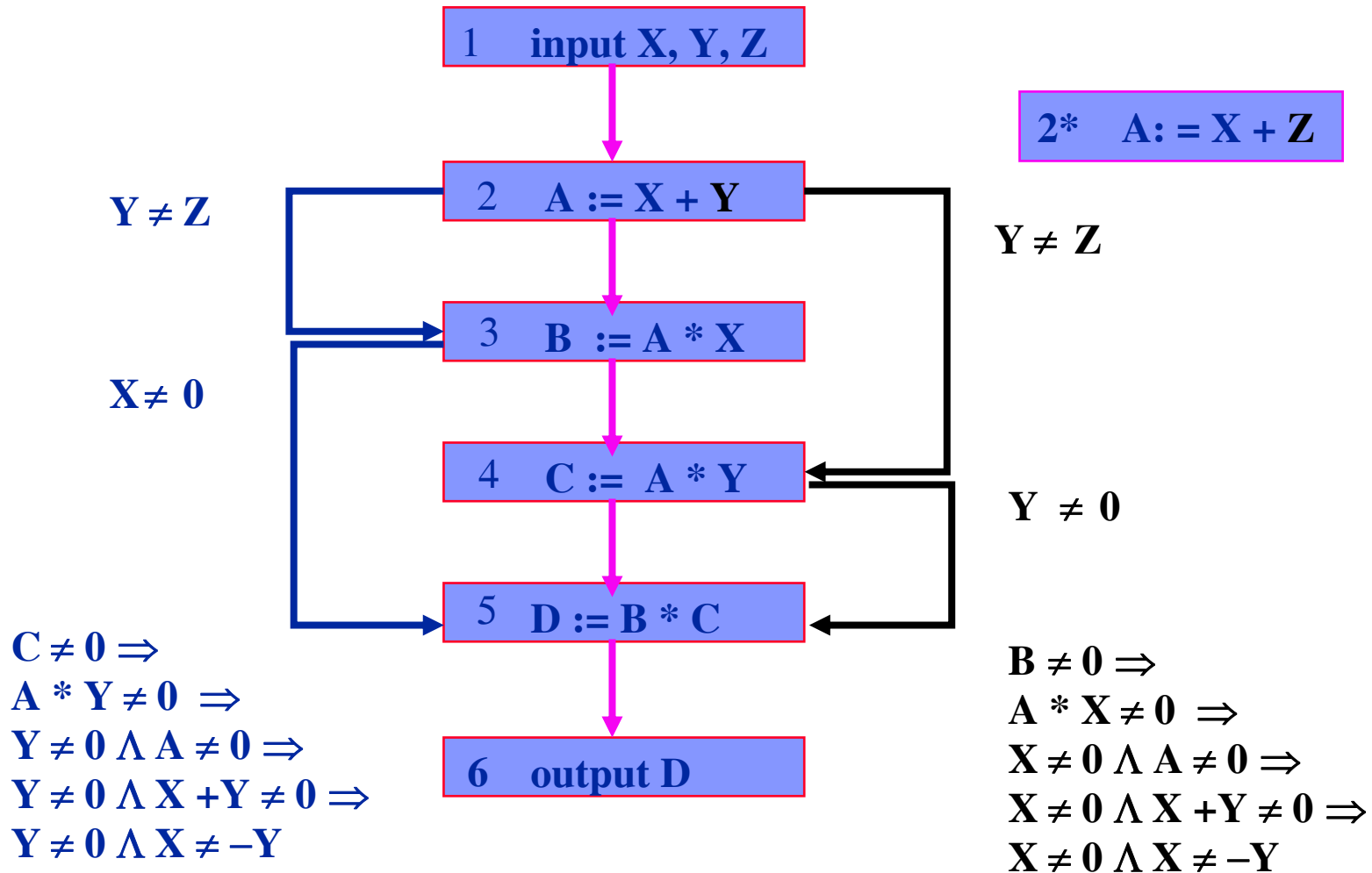
## Step 1b

- computational transfer condition for a statement
  - $\text{exp1} \langle \text{op} \rangle \text{exp2} \neq \text{exp1}' \langle \text{op} \rangle \text{exp2}$
  - defined for operator and fault
    - e.g.,  $(b + c) \neq (b + 1) \Rightarrow c \neq 1$
  - many are fault independent
    - $c * (\text{exp}) \neq c * (\text{exp}')$   
 $\Rightarrow c \neq 0$

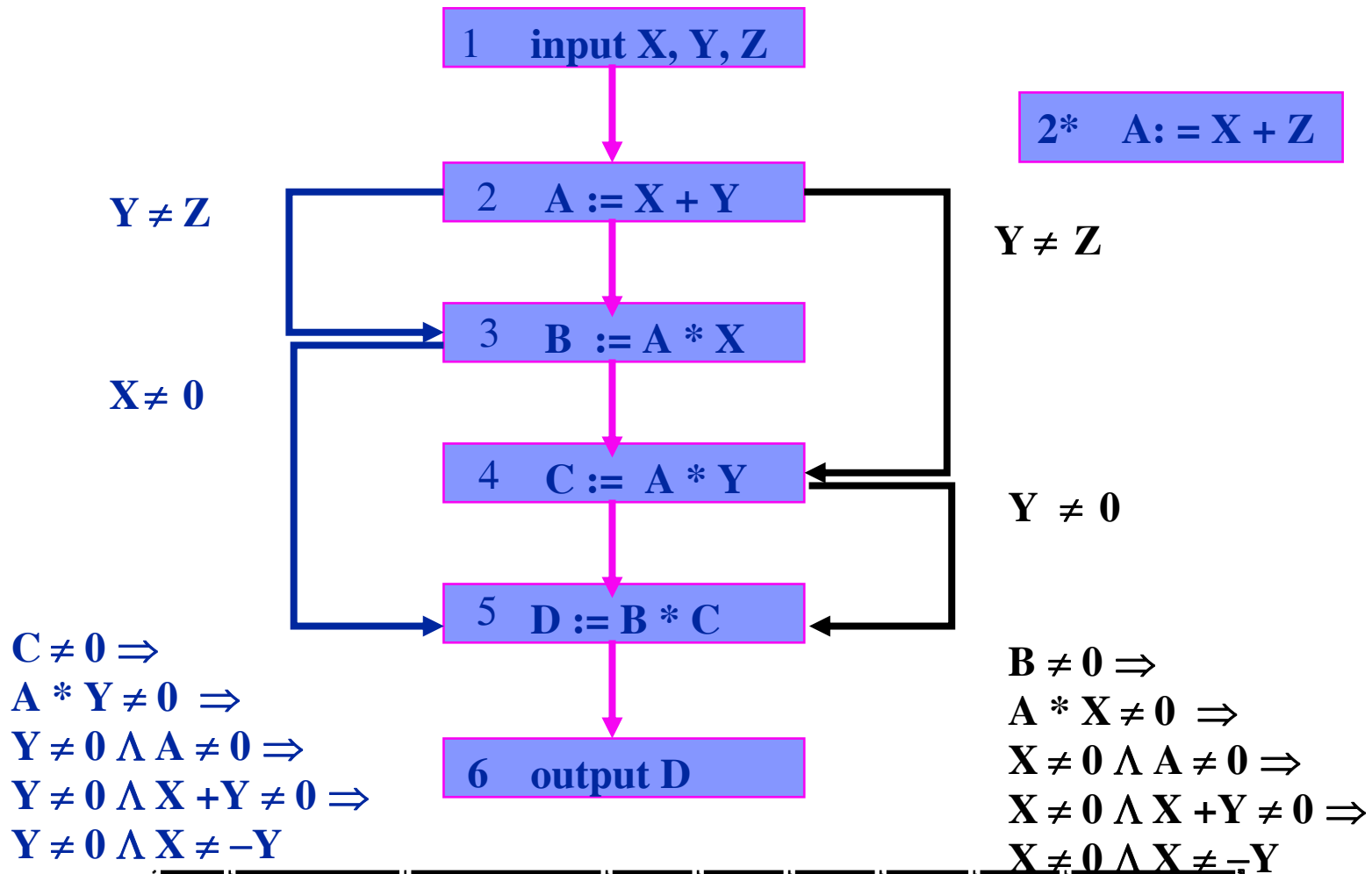
## Step 2

- **Information flow transfer**
  - combines data dependence and control dependence transfer
  - occurs along information flow chains
  - to guarantee transfer from (hypothetically) faulty node to output must guarantee transfer along transfer set
    - collection of information flow chains that can be executed together

# Simpler Example

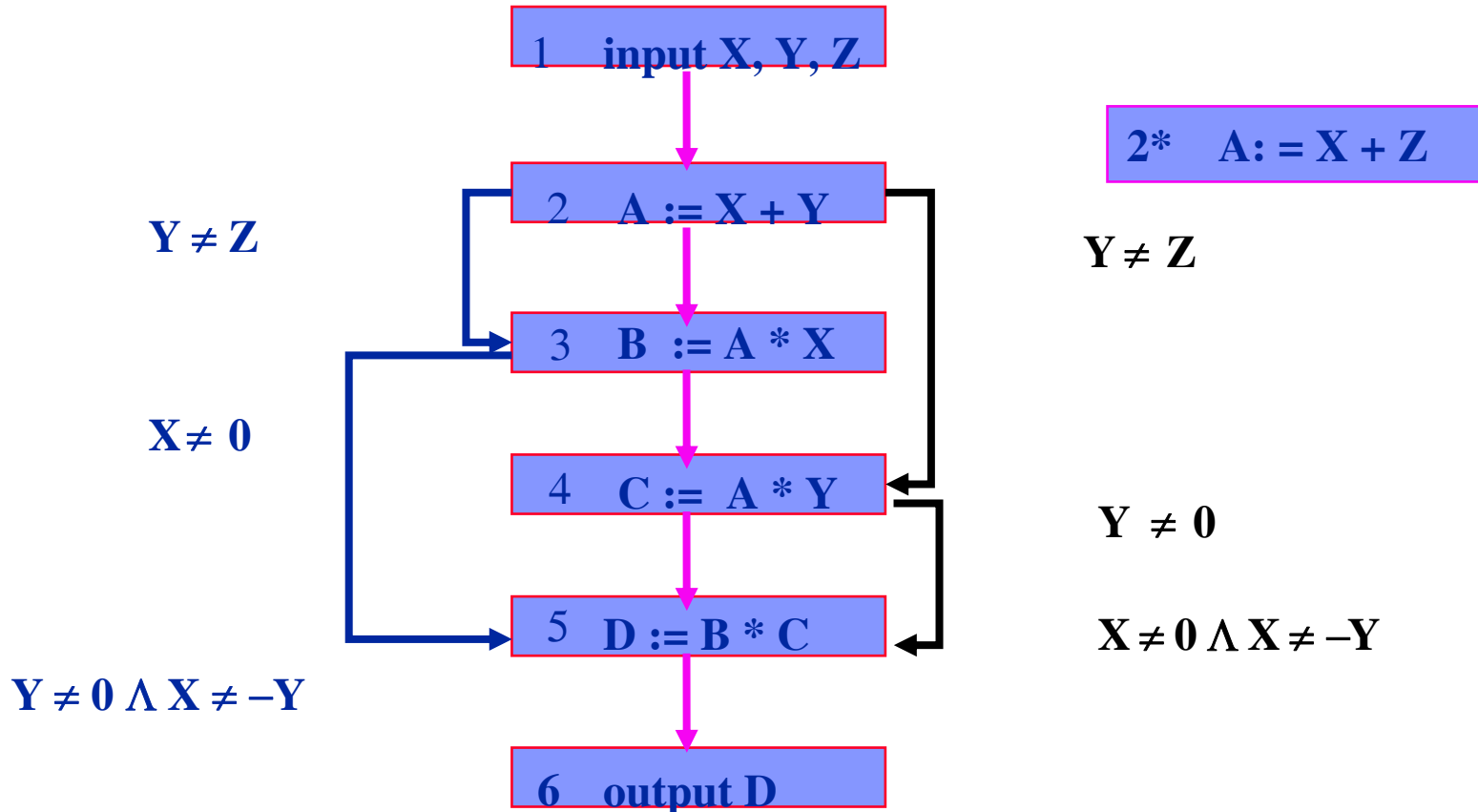


# Necessary but not sufficient?



	module	test case			a	b	c	d	output
		x	y	z					
x+y	faulty	1	-3	1	-2	-2	6	-12	-12
x+z	correct	1	-3	1	2	2	-6	-12	-12

# Not Necessary!



	module	test case		<i>a</i>	<i>b</i>	<i>c</i>	<i>d</i>	<i>output</i>		
		x	y	z						
x+y	1	faulty	1	-3	1	-2	-2	6	-12	-12
x+z		correct	1	-3	1	2	2	-6	-12	-12
x+y	2	faulty	1	-1	1	0	0	0	0	0
x+z		correct	1	-1	1	2	2	-2	-4	-4

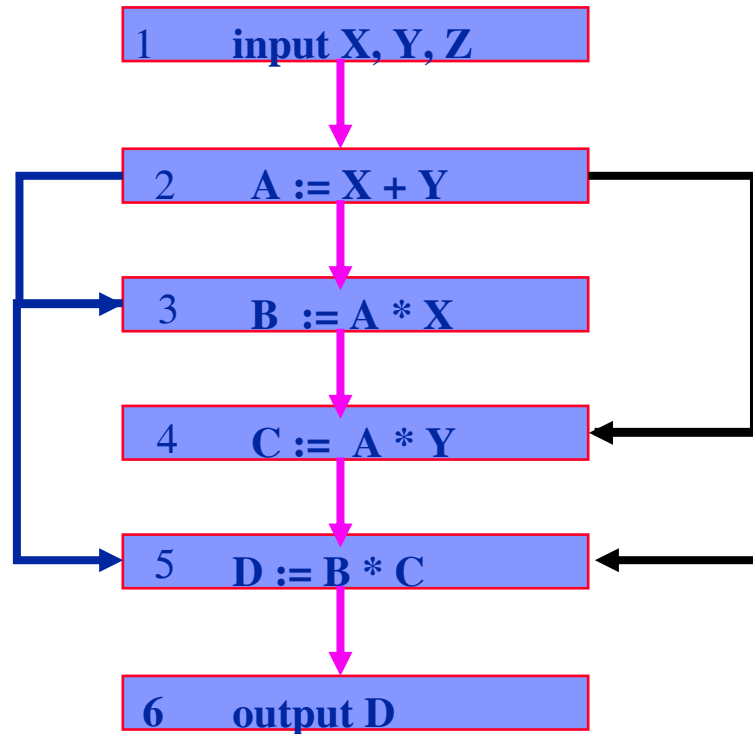
# Transfer Condition

- condition that guarantees transfer
  - must know points of interaction
    - places where two or more potential failures come together
- Transfer set defines locations of potential interaction
  - Notation:  $(U_n, V_m)$  means faulty value for variable  $U$  at node  $n$  transfers to variable  $V$  at node  $m$
- Transfer route defines chains of transfer set elements that can be combined to form a path



# Example

- Transfer Set =  
 $\{(A_2, B_3), (B_3, D_5), (D_5, \text{out}_6), (A_2, C_4) (C_4, D_5) \}$



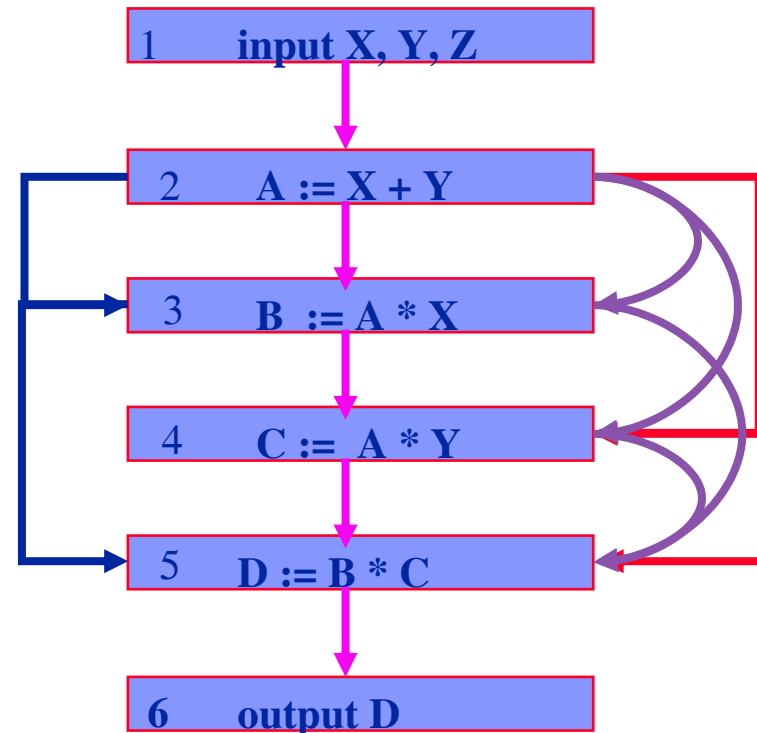
Notation:  $(U_n, V_m)$  means faulty value for variable  $U$  at node  $n$  transfers to variable  $V$  at node  $m$

## Construction of Transfer Route

- different ways to transfer along same set, depending on which portions of chains transfer and which do not
- a transfer route is a subset of the nodes in a transfer set where transfer does and **does not** occur
- a transfer route defines where actual interactions occur

# Example

- Transfer Set =  
 $\{(A_2, B_3), (B_3, D_5), (D_5, \text{out}_6), (A_2, C_4), (C_4, D_5)\}$
- Transfer Routes
  1. (A transfers to B at 3) and  
(A does not transfer to C at 4)  
and (B transfers to D at 5)
  2. (A does not transfer to B at 3)  
and (A transfers to C at 4)  
and (C transfers to D at 5)
  3. (A transfers to B at 3) and  
(A transfers to C at 4) and  
(B and C transfer to D at 5)

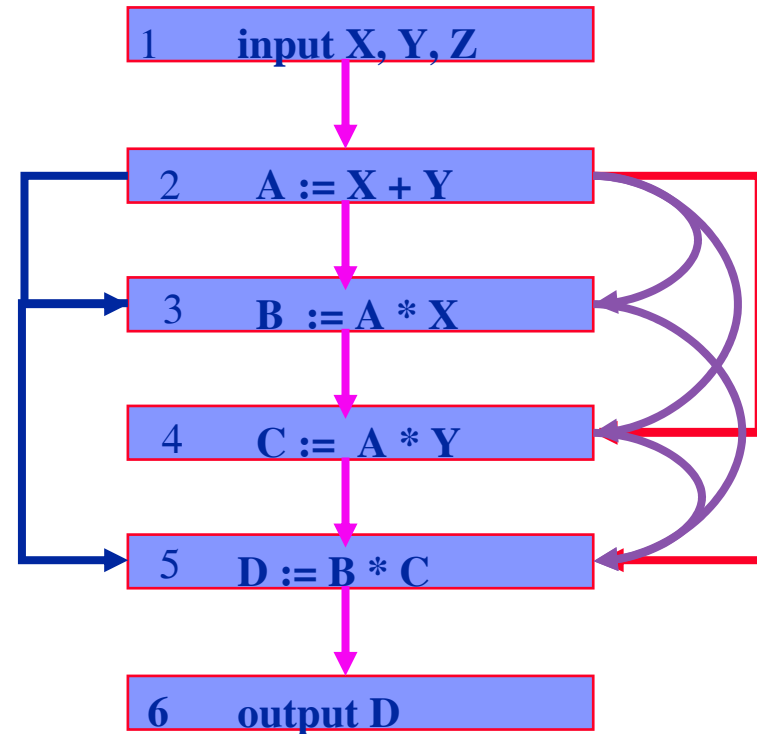


# Transfer Condition

- 1. Path Condition
  - guarantees execution of a particular transfer route
    - must guarantee execution of nodes in chain as well as def-clear paths between nodes
- 2. Transfer Route Condition
  - guarantees transfer for particular transfer route
    - computational transfer conditions at nodes in transfer route where transfer **does** occur
    - complement of computational transfer conditions at nodes where transfer **does not** occur

# Transfer Routes for Example

1. (A transfers to B at 3) and  
(A does not transfer to C at 4) and  
(B transfers to D at 5)
2. (A does not transfer to B at 3) and  
(A transfers to C at 4) and  
(C transfers to D at 5)
3. (A transfers to B at 3) and  
(A transfers to C at 4) and  
(B and C transfer to D at 5)



# Condition for First Transfer Route

(A transfers to B at 3) and  
(A does not transfer to C at 4) and  
(B transfers to D at 5)

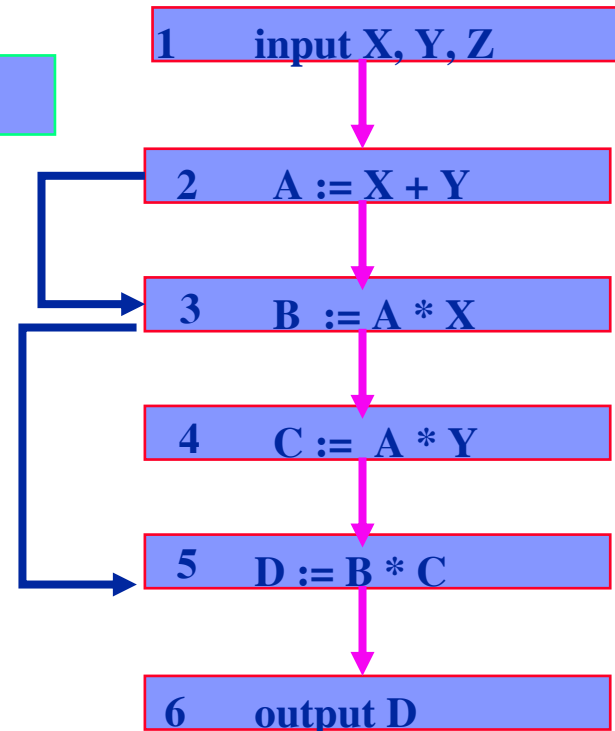
- **Transfer Route**

**Conditions:**

$x \neq 0 \wedge y = 0 \wedge c \neq 0 \Rightarrow$

$x \neq 0 \wedge y = 0 \wedge a*y \neq 0 \Rightarrow$  **false**

2\* A := X + Z



# Condition for Second Transfer Route

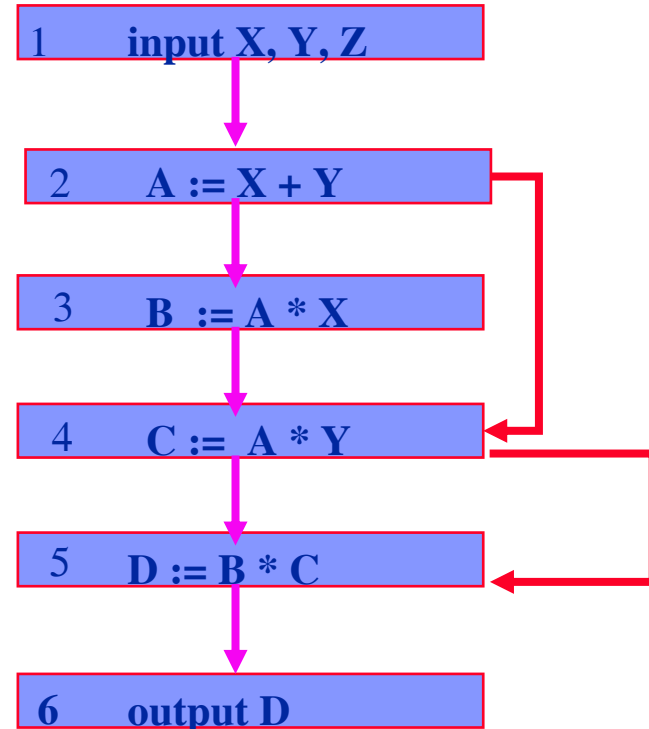
(A does not transfer to B at 3) and  
(A transfers to C at 4) and  
(C transfers to D at 5)

- **Transfer Route Conditions:**

$x = 0 \wedge y \neq 0 \wedge b \neq 0 \Rightarrow$

$x = 0 \wedge y \neq 0 \wedge a * x \neq 0 \Rightarrow$  false

2\* A := X + Z



# Condition for Third Transfer Route

(A transfers to B at 3) and  
(A transfers to C at 4) and  
(B and C transfer to D at 5)

## • Transfer Route Conditions:

$$x \neq 0 \wedge y \neq 0 \wedge b * c \neq b' * c' \Rightarrow$$

$$x \neq 0 \wedge y \neq 0 \wedge (a*x)(a*y) \neq (a'*x)(a'*y) \Rightarrow$$

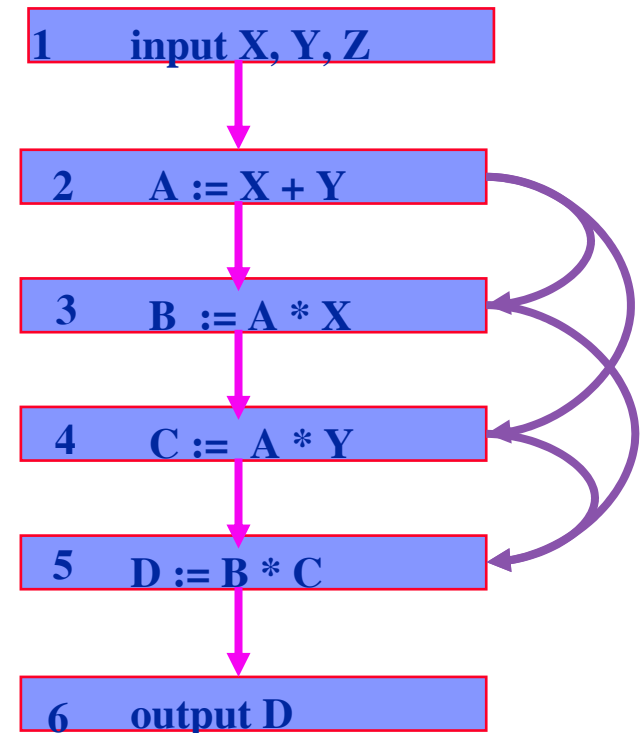
$$x \neq 0 \wedge y \neq 0 \wedge$$

$$(x+y)x(x+y)y \neq (x+z)x(x+z)y \Rightarrow$$

$$x \neq 0 \wedge y \neq 0 \wedge (x+y)^2 \neq (x+z)^2 \Rightarrow$$

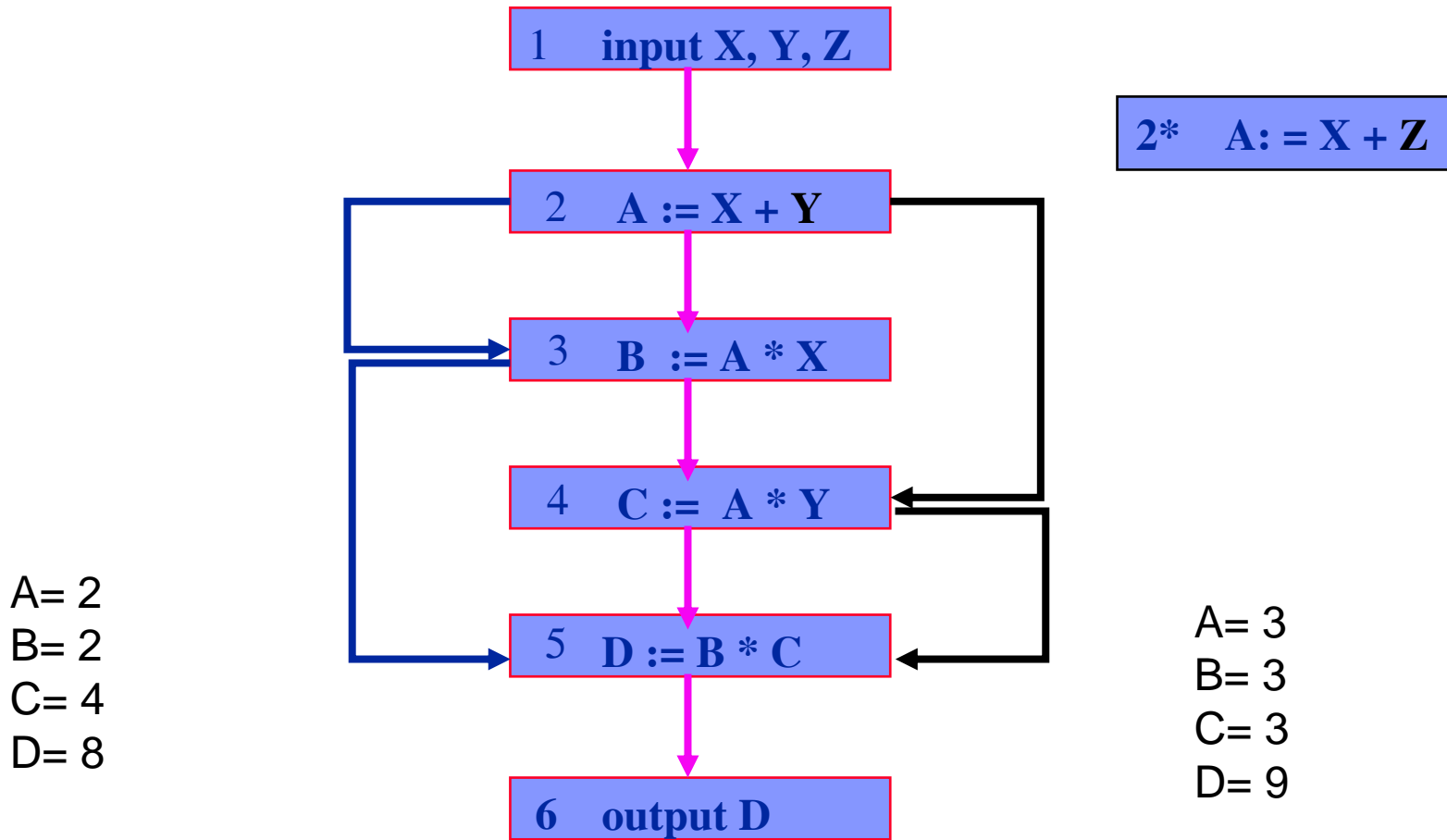
$$x \neq 0 \wedge y \neq 0 \wedge y \neq z$$

test case:  $x=1, y=1, z=2$  satisfies the conditions and causes the fault to be revealed





# Example



test case:  $x=1, y=1, z=2$  satisfies the conditions  $x \neq 0 \wedge y \neq 0 \wedge y \neq z$  and causes the fault to be revealed

# Failure condition

*failure condition =*

*original state potential failure condition **and** transfer condition*

if test data satisfies failure condition (fc) and failure → fault

if test data satisfies fc and no failure → no fault

if can't satisfy fc → try another transfer set

if can't satisfy fc for all transfer sets → no fault

## Relay Fault Based Approach

- recognizes what is needed to transfer to output
- other fault based techniques:
  - do not deal with how to select test data that transfers
  - may recognize need to transfer but provide no guidance in test data selection (assume transfer "usually" occurs)
  - do not consider control dependence
  - none discuss interactions for a single fault/multiple faults -- they assume that there is a single fault or if there is more than one that there is no interaction

## Relay Fault Based Approach

- defines what is needed to reveal a fault at a statement
  - a general procedure that could be applied to any "atomic" fault
- defines what is needed to propagate erroneous values to output
  - **a very negative result!**
  - if interaction is not accounted for, then the constraints are neither necessary nor sufficient
  - assumptions about single faults are now very questionable
  - can not assume constraints are necessary